

Extension	Efficiency
1	0.6098
2	0.8544
3	0.9663
4	0.9837
5	0.9926

Table 1. Efficiencies of {0.85, 0.15} Huffman code extensions

Extension	Efficiency
1	0.7219
2	0.9255
3	0.9917
4	0.9745
5	0.9783

Table 2. Efficiencies of {0.80, 0.20} Huffman code extensions

Ext =	1	2	3	4	5	6	7
0.05		0.2864	0.4992	0.6610	0.7800	0.8519	0.9056 0.9429
0.10		0.4690	0.7271	0.8805	0.9522	0.9767	0.9975 <u>0.9887</u>
0.15		0.6098	0.8544	0.9663	0.9837	0.9926	<u>0.9817</u> 0.9914
0.20		0.7219	0.9255	0.9917	<u>0.9745</u>	0.9783	0.9954 <u>0.9866</u>
0.25		0.8113	0.9615	0.9859	0.9913	0.9921	<u>0.9910</u> 0.9932
0.30		0.8813	0.9738	<u>0.9699</u>	0.9882	0.9913	0.9922 0.9964
0.35		0.9341	0.9692	0.9840	<u>0.9836</u>	0.9963	<u>0.9896</u>
0.9963							
0.40		0.9710	0.9710	0.9894	0.9896	0.9931	0.9945 0.9955
0.45		0.9928	0.9928	0.9928	0.9929	0.9946	0.9951 0.9959

Table 3. Efficiencies for extensions of a range of binary codes

$\epsilon$	0.0	0.1	0.2	0.3	0.4	0.5
Ext = 1		.....	.....	.....	.....	.....
2		.....	.....	.....	.....	.....
3		.....	.....	.....663.....	.....	.....
4		.....	.....688886.....	.....134554.....	.....	.....
5		.....	.....	.....	.....	.....
6		.....1777.....	.....43.....	.....57777651.....	.....	.....
7		.....57887.....	.....677652.....	.....	.....	.....
8		.....3666.....	.....455432.....	.....5666654.....	.....	.....
9		.....	.....	.....	.....43.....	.....

Table 4. Efficiency losses for extensions of a range of binary codes

	$P(A) = 0.35; P(B) = 0.65$	Length for $P(A) = \epsilon$	$P(A) = 0.45; P(B) = 0.55$
BB	0.4225 0	$(1-\epsilon)^2$	0.3025 11
BA	0.2275 10	$2\epsilon(1-\epsilon)$	0.2475 10
AB	0.2275 111	$3\epsilon^2(1-\epsilon)$	0.2475 01
AA	0.1225 110	$3\epsilon^3$	0.2025 00

Table 5. Huffman codes for probabilities of 0.35 and 0.45

Probability range	codeword lengths	Average codeword lengths
$0.00 < \epsilon < 0.30$	{4, 4, 4, 4, 3, 3, 3, 1}	$L = 2\epsilon^3 + 6\epsilon + 1$
$0.30 < \epsilon < 0.34$	{4, 4, 4, 4, 3, 3, 2, 2}	$L = 2\epsilon^3 + 2\epsilon^2 + 2\epsilon + 2$
$0.34 < \epsilon < 0.44$	{4, 4, 3, 3, 3, 3, 3, 2}	$L = \epsilon^3 + 2\epsilon^2 + 3\epsilon + 2$
$0.44 < \epsilon < 0.50$	{3, 3, 3, 3, 3, 3, 3, 3}	$L = 3$

Table 6. Code trees and word lengths for third extension

		P(A)				
		0.1	0.2	0.3	0.4	0.5
		-----:----- -----:----- -----:----- -----:----- -----:-----				
	0.01	.....	.....	44.....	.....	4444
	0.02	.....	.....	44.....	.....	44444444
	0.03	.....	.....	444444	.....	44444444
	0.04	.....	.....	44444444	.....	44444444
	0.05	.....	.....	444444444444	.....	44444444
	0.06	.....	.....	4444444444444444	.....	44444444
	0.07	.....	.....	4444444444444444	.....	44444444
	0.08	.....	.....	4444444444444444	.....	.....
	0.09	.....	.....	4444444444444444	.....	.....
	0.10	.....	.....	4444444444444444	.....	.....
	0.11	.....	.....	444444444444	.....	.....
	0.12	.....	.....	4444444444	.....	.....
P(B)	0.13	.....	.....	444444	.....	33.....
	0.14	.....	.....	44	.....	333333.....
	0.15	.....	.....	33333333	.....	.....
	0.16	.....	.....	333333333333	.....	.....
	0.17	.....	.....	3333333333333344	.....	.....
	0.18	.....	.....	33333333333334	.....	.....
	0.19	.....	.....	333333333333	.....	.....
	0.20	.....	.....	<u>3</u> 3333333333	.....	.....
	0.21	.....	.....	3333333333	.....	.....
	0.22	.....	.....	3333333	.....	.....
	0.23	.....	.....	33333	.....	.....
	0.24	.....	.....	33	.....	.....
	0.25	.....	.....	.	.....	.....

Table 7. Anomalies for ternary Huffman codes

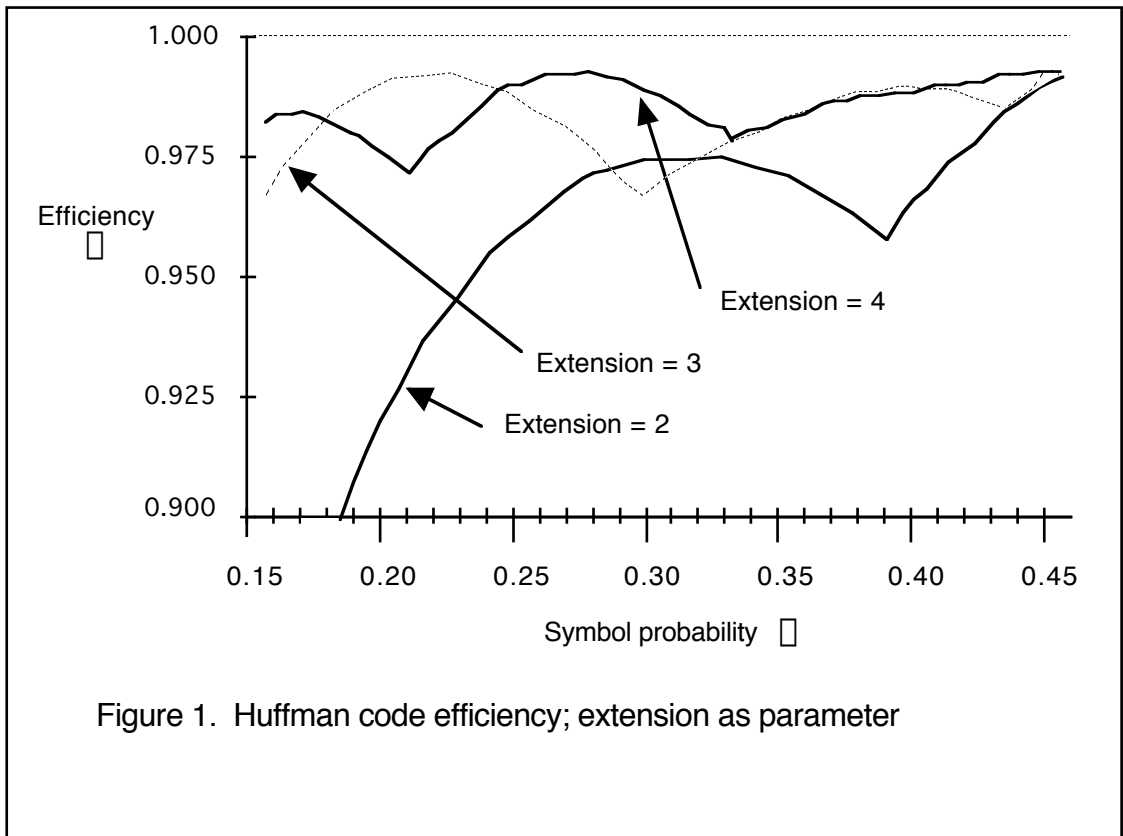


Figure 1. Huffman code efficiency; extension as parameter

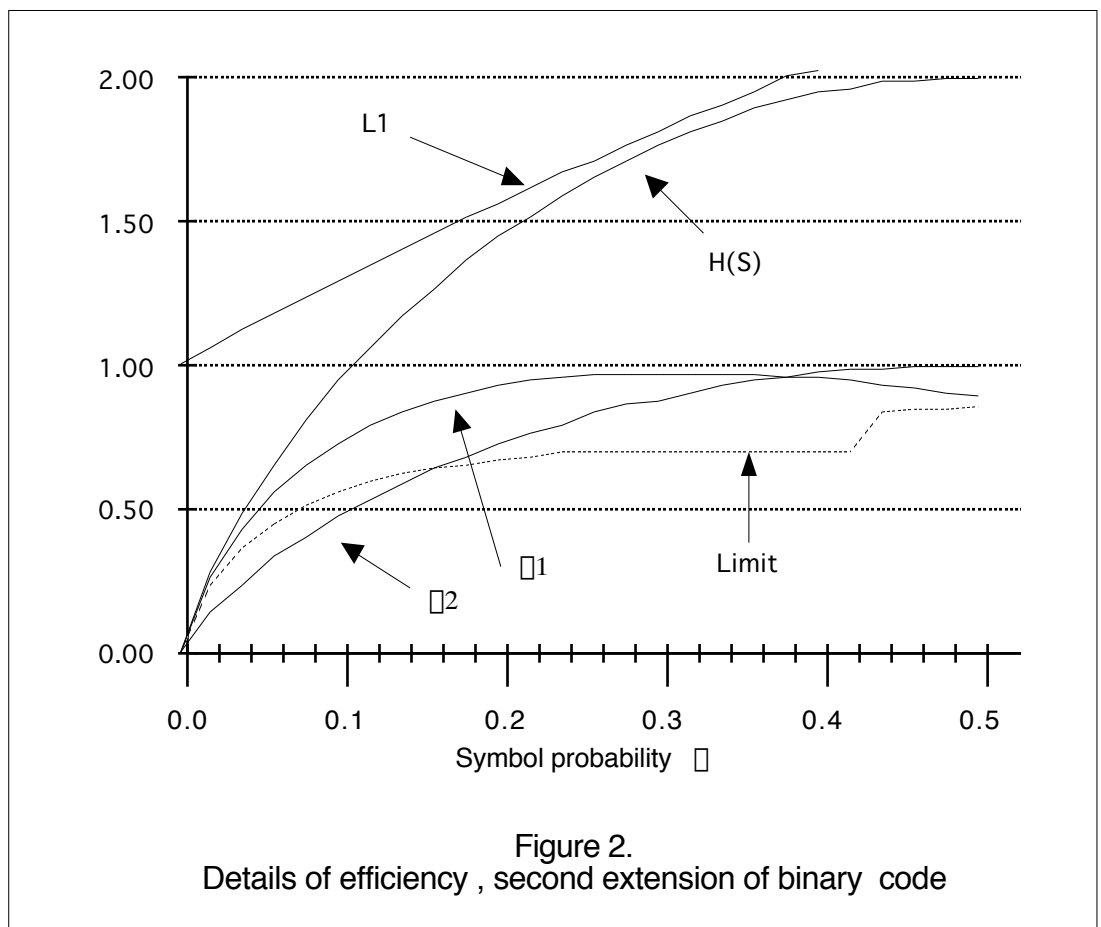


Figure 2. Details of efficiency, second extension of binary code