

Here are corrected versions of Figures 5.7, 5.9, 5.10 of the textbook. There was an error caused by cutting and pasting, and forgetting to edit. In fact Figure 5.9 has not changed at all — in the case of BFS we can get away with colouring all white neighbours grey in one step, but we clearly cannot in the other cases.

An important issue not properly discussed in the book is: how do we check whether a node u has a white neighbour v ? It seems that in the worst case we might need to scan all neighbours of u until we find a white one. This would ruin the linear running time of DFS, for example. An easy way to fix this is, each time we colour v grey, to delete v from the adjacency list of u .

```

algorithm dfs
  Input: digraph  $G$ 
begin
  stack  $S$ 
  array  $colour[n], pred[n], seen[n], done[n]$ 
  for  $u \in V(G)$  do
     $colour[u] \leftarrow \text{WHITE}; pred[u] \leftarrow \text{NULL}$ 
  end for
   $time \leftarrow 0$ 
  for  $s \in V(G)$  do
    if  $colour[s] = \text{WHITE}$  then
      dfsvisit( $s$ )
    end if
  end for
  return  $pred, seen, done$ 
end

algorithm dfsvisit
  Input: node  $s$ 
begin
   $colour[s] \leftarrow \text{GREY}$ 
   $seen[u] \leftarrow time; time \leftarrow time + 1$ 
   $S.insert(s)$ 
  while not  $S.isempty()$  do
     $u \leftarrow S.get\_top()$ 
    if there is a neighbour  $v$  with  $colour[v] = \text{WHITE}$  then
       $colour[v] \leftarrow \text{GREY}; pred[v] \leftarrow u$ 
       $seen[v] \leftarrow time;$ 
       $S.insert(v)$ 
    else
       $S.delete()$ 
       $colour[u] \leftarrow \text{BLACK}$ 
       $done[u] \leftarrow time; time \leftarrow time + 1$ 
    end if
  end while
end

```

Figure 1: Depth-first search algorithm.

```

algorithm bfs
  Input: digraph  $G$ 
begin
  queue  $Q$ 
  array  $colour[n], pred[n], d[n]$ 
  for  $u \in V(G)$  do
     $colour[u] \leftarrow \text{WHITE}; pred[u] \leftarrow \text{NULL}$ 
  end for
  for  $s \in V(G)$  do
    if  $colour[s] = \text{WHITE}$  then
      bfsvisit( $s$ )
    end if
  end for
  return  $pred, d$ 
end

algorithm bfsvisit
  Input: node  $s$ 
begin
   $colour[s] \leftarrow \text{GREY}; d[s] \leftarrow 0$ 
   $Q.insert(s)$ 
  while not  $Q.isempty()$  do
     $u \leftarrow Q.get\_head()$ 
    for each  $v$  adjacent to  $u$  do
      if  $colour[v] = \text{WHITE}$  then
         $colour[v] \leftarrow \text{GREY}; pred[v] \leftarrow u; d[v] \leftarrow d[u] + 1$ 
         $Q.insert(v)$ 
      end if
    end for
     $Q.delete()$ 
     $colour[u] \leftarrow \text{BLACK}$ 
  end while
end

```

Figure 2: Breadth-first search algorithm.

```

algorithm pfs
  Input: digraph  $G$ 
begin
  priority queue  $Q$ 
  array  $colour[n], pred[n]$ 
  for  $u \in V(G)$  do
     $colour[u] \leftarrow \text{WHITE}; pred[u] \leftarrow \text{NULL}$ 
  end for
  for  $s \in V(G)$  do
    if  $colour[s] = \text{WHITE}$  then
      pfsvisit( $s$ )
    end if
  end for
  return  $pred$ 
end

algorithm pfsvisit
  Input: node  $s$ 
begin
   $colour[s] \leftarrow \text{GREY}$ 
   $Q.insert(s, setkey(s))$ 
  while not  $Q.isempty()$  do
     $u \leftarrow Q.get\_min()$ 
    if  $u$  has a neighbour  $v$  with  $colour[v] = \text{WHITE}$  then
       $colour[v] \leftarrow \text{GREY}$ 
       $Q.insert(v, setkey(v))$ 
    else
       $Q.delete\_min()$ 
       $colour[u] \leftarrow \text{BLACK}$ 
    end if
  end while
end

```

Figure 3: Priority-first search algorithm (first kind).