Predicting FPP elections

Mark C. Wilson CMSS seminar October 6, 2015

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- FPP is known to lead to very disproportional outcomes, where the seat share of a party can vary hugely from its overall national vote share.
- This system is strongly associated with British colonization. Used in UK, Canada, USA, India (was used in NZ until 1993).

Other countries using FPP for parliamentary elections

Antigua and Barbuda, Bahamas, Bangladesh, Barbados, Belize, Bermuda, Bhutan, Botswana, Burma, Dominica, Ghana, Grenada, Jamaica, Kenya, Malawi, Malaysia, Nigeria, Pakistan, St Kitts and Nevis, St Lucia, St Vincent and the Grenadines, Trinidad and Tobago, Uganda, Zambia.

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- Azerbaijan, Ethiopia, Gambia, Ivory Coast, Liberia, Maldives, Federated States of Micronesia, Palau, Sierra Leone, Solomon Islands, Tanzania, Yemen.

Plurality ballots - no further preferences can be expressed

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Choose ONE candidate to EXECUTE by placing an X next to his name.

SIMON COWELL	
SEPP BLATTER	
GEORGE OSBORNE	
GORDON RAMSAY	
RUPERT MURDOCH	

FPP often distorts the vote-seat ratio

First Past the Post Explained

UKIP 3.8m votes = 1 MP Greens 1.1m votes = 1 MP SNP 1.5m votes = 56 MPs

Numbers as of 10.45am Friday 8 May

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- This is said to be the closest thing to a scientific law in political science. There are exceptions.
- Strategic voting is very common in FPP elections "voting for a loser is a wasted vote".

Prediction is becoming a big industry. The UK2015 election had at least 10 academic and media teams delivering predictions many times before the election.

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- There is a huge demand for polling by news media.
- Poll information is often used to determine candidate and party viability and has impact on fundraising. Polls can be self-reinforcing.
- For political scientists, predictions serve to help refine their models of voter preferences. This is more important than just getting the right answer.

Predicting FPP elections

Methodological issues

There is no agreed measure of format of prediction.

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- There is no agreed measure of prediction accuracy.
- All predictions involve uncertainty, but how to estimate it, and convey this to the public?

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How many seats will each party win?

Types of prediction

Which party or parties will form the government?

- How many seats will each party win?
- Which party will win each seat?

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- Which party or parties will form the government?
- How many seats will each party win?
- Which party will win each seat?
- Predictions can be point estimates or probability distributions.

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- "... eleven election forecasting teams gathered today (27th March) at a major conference at the LSE on the eve of the 2015 general election campaign. The different teams are all agreed that Britain is heading for a hung parliament on May 7th." (LSE blog)
- In reality Conservatives obtained an absolute majority of seats.

US Presidential election 1948



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US Presidential election 2012



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- ► FPP itself magnifies small differences in party support.
- The US system has an extra level (Electoral College) which amplifies small differences even more.
- There are not many data points for statistical techniques to work on, yet it is very complicated to model voter behaviour very accurately.

Possible input variables other than voting intention polls

• Margin of victory of main party leader in leadership election.
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- District-level polls are usually restricted to districts in which the result is expected to be close.
- Even if national opinion polls (random sampling of voting intentions) give a completely accurate result, we don't know what is happening in each district.

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- The most basic predictions simply compute each seat result based on the votes from last election and the district-level votes imputed by using the swing hypothesis and poll data.
- We call this the default model. Any more complicated model based on voting intention polls should do at least as well as this in order to be credible.

Models behind the two hypotheses

► AS is based on the idea of voter flows between parties. If 1% of eligible voters switch from X to Y then this happens in each district.

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- MS requires changes in the total numbers of voters (so can account for turnout changes?) but AS does not.

Example

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We have

$$A(x_i, \varepsilon) = x_i + \varepsilon/2$$
$$M(x_i, \varepsilon) = \frac{x_i(1+\varepsilon)}{1+\varepsilon(2x_i-1)}.$$

Example continued

ε	x_i	$A(x_i,\varepsilon)$	$M(x_i,\varepsilon)$
-1	0.3	-0.2	0
-0.1	0.3	0.25	0.2596
0.1	0.3	0.35	0.3438
1	0.3	0.8	1
ε	0.5	$(1+\varepsilon)/2$	$(1+\varepsilon)/2$
-0.2	0.6	0.5	0.5
0.2	0.6	0.7	0.6923
0.5	0.6	0.9	0.8682

• $A(x_i, \varepsilon) - M(x_i, \varepsilon)$ has degree 4 Taylor expansion about (1/2, 0) equal to $\varepsilon^2(x - 1/2) + 2\varepsilon(x - 1/2)^2$.

• $A(x_i, \varepsilon) - M(x_i, \varepsilon)$ has maximum value 0.5, minimum -0.5.

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- AS seems to be much more popular in the UK prediction community, but I don't really understand why.
- Many models use one of these as a base, but do a lot of possibly ad hoc work in order to make use of extra information (which is often biased or has large error). This includes models of poll bias and voter dishonesty, district-level polls.

Which of the two swing hypotheses explains the data better?

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- ▶ We can predict election i + 1 using the default model based on election i, and opinion polls (averaged somehow, which is a big issue). We can then try to optimize the poll date relative to the election - there is some evidence that it should not be the latest possible.

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- There are many distances on probability distributions, for example the total variation metric. If we can measure distance between parties then a Wasserstein distance is appropriate.
- Another measure is the number of seats whose result was correctly predicted (for those models that give this detail).
- I have not yet analysed the UK2015 predictions to see whether they outperformed the default model. Note that the default model was not run separately on regions (Scotland, Wales).

Point predictions for the UK 2015 election (632 GB seats)

Predictor	date	CON	LAB	LIB	UKIP	GREEN	SNP
previous	20100506	306	258	57	0	1	6
real	20150507	330	232	8	1	1	56
Hanretty	20150507	278	267	27	1	1	53
Fisher	20150507	285	262	25	0	1	53
default (AS)	20150508	328	277	15	0	1	7
default (MS)	20150508	332	258	0	0	3	34

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 Relatively small changes in projected vote shares make a big difference in seat projections.

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 - (MS): CON 142, NDP 86, LIB 105, BQ 4, GRE 1
- Using the CBC/ThreeHundredEight.com from yesterday gives

- (AS): CON 135, NDP 102, LIB 96, BQ 4, GRE 1
- (MS): CON 126, NDP 96, LIB 113, BQ 2, GRE 1

- Relatively small changes in projected vote shares make a big difference in seat projections.
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- It seems likely that CON will be the biggest party, no party will have a majority, and BQ will have very few seats. All forecasters are predicting the same thing, to my knowledge.

If there was no change in voting behaviour, a switch to proportional representation would benefit BQ and Green the most, be very good for LIB, not much different for NDP, very bad for CON.

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- The current seat allocations are: CON 166, NDP 103, LIB 34, BQ 4, GRE 1. Scaled up to the current Parliament size this is: CON 182, NDP 113, LIB 37, BQ 5, GRE 1.

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- It is easy to predict who will (not) be advocating PR after this election. CON seem to be better at winning seats by small margins than other parties.