#### MMP review submission

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# 2012 MMP review

The Electoral Commission of New Zealand solicited submissions on several aspects of the MMP electoral system, as discussed at Arkadii Slinko's talk in Semester 1.e

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- After over 4000 initial submissions, they produced a Proposal Paper that proposed only the following changes: reduce party vote threshold to 4%; remove one electorate seat threshold; remove the "overhang" seats.
- http://mmpreview.org.nz/ contains much information on the process.

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- We were not convinced by the Commission's arguments for the optimality of this value.
- We aimed to compute measures of overall system quality under various assumptions on voter preferences.
- ▶ We investigated values of threshold from 0 to 8%, and interpret our results as showing that 4% is considerably too high.

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#### Background

#### Measures of system quality: proportionality

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- There are many disproportionality indices in the literature. Many relate strongly to an apportionment method. Each is computed using the vote fraction v<sub>i</sub> and seat fraction s<sub>i</sub> awarded to each party, i.

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- There are many disproportionality indices in the literature. Many relate strongly to an apportionment method. Each is computed using the vote fraction v<sub>i</sub> and seat fraction s<sub>i</sub> awarded to each party, i.
- We use the Loosemore-Hanby index (related to Hamilton's method),

$$L = \frac{1}{2} \sum_{i} |v_i - s_i|$$

and the Gallagher index,

$$G = \left(\frac{1}{2}\sum_{i}(v_i - s_i)^2\right)^{1/2}$$

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It makes sense to us to use a modified version that takes into account power, rather than just presence in Parliament. We replace the fraction s<sub>i</sub> above by the Shapley-Shubik power index σ<sub>i</sub>. This index has an interpretation in terms of a noncooperative bargaining model.

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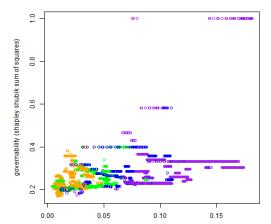
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- We assume no difference in strategic voter behaviour, or party behaviour.

# Results: Loosemore-Hanby/Shapley-Shubik

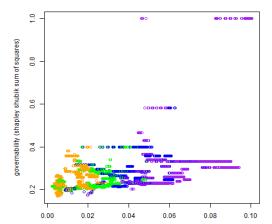
Figure: 2% (orange), 3% (green), 4% (blue), 5% (purple)



0.02 - 0.05

# Results: Gallagher/Shapley-Shubik

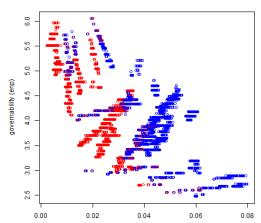
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# Results: Gallagher/Laakso-Taagepara

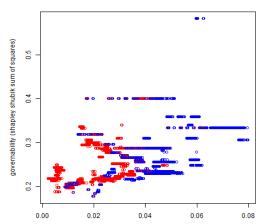
Figure: 3% (red) versus 4% (blue)



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Research questions

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- What does it mean to generate "realistic" hypothetical elections?
- Which formal measures of robustness of results should we use, if any?

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