



# CS.760

## Case-Based Reasoning 6 Dr. Ian Watson

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## Contents

- Testing & evaluation
  - Leave one out
  - Leave one in
  - Global system metrics
- Case competence
  - The Competence Issue
  - A Competence Model for CBR
  - Case Discovery – competence holes
  - Discussion

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## Testing

- Testing an ML algorithm is easy (boring but easy)
  - Obtain a data set
  - Divide into training & test data
  - Train your classifier
  - Run the classifier on the test set
- Not so straightforward with CBR

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## Testing

- What are we testing?
- The retrieval (classification) accuracy?
  - Then ML methodology is appropriate
- The adaptation accuracy?
  - Validate the accuracy of the generated solution
- The combined accuracy (retrieval & adaptation)
- What about efficiency, speed?
- Also a case-base changes with time....

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## Testing

- The performance of a CBR system is the product of a combination of processes
- To test one in isolation may give spurious results
- Difficult to scientifically test all together
- But there are some useful simple tests

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## Testing

- Leave one out testing
  - For  $i = 1$  to  $n$  (where  $n = \text{No. cases}$ )
  - Remove case <sub>$i$</sub>  and use as a query case
- Useful for finding outlying cases
- Useful for finding dense areas of the case-base

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## Testing

- Leave one in testing
  - For  $i = 1$  to  $n$  (where  $n = \text{No. cases}$ )
    - Do NOT Remove case $_i$  but use as a query case
- query-case should exactly match case $_i$
- Also useful for finding outlying cases
- Also useful for finding dense areas of the case-base

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## Testing

- Global system tests
  - Considers accuracy as well as performance issues
  - Since a case-base changes with time
  - Create a reference set of cases
  - Log performance data using this reference set over time
  - Useful way of monitoring relative performance

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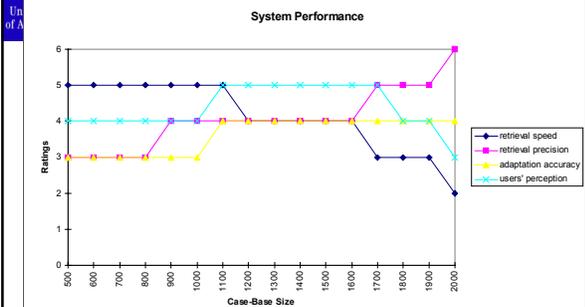
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 **Testing**

- No point in testing if you know you have a “bad” case-base
- The best retrieval and adaptation algorithms will not work well on a “bad” case base
- But what is a bad or a good case-base?

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 **Characterizing a case-base**

- Motherhood statements....
  - The case-base should be “representative”
  - The cases should be “well” distributed
  - Cases should be useful
- Doesn't really help us much
- Hence case competence models
  - University College Dublin (Barry Smyth)

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 **What is performance**

- Performance = Competence + Efficiency
- In pure CBR
  - Cases contribute to *both* competence and efficiency

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## Recent Developments in CBR

- Real-World Applications
  - Large Scale Case-Bases
  - On-Line Learning
- Emerging Issues
  - The Utility Problem
    - More cases decreases the utility of individual cases
  - Case-Base Maintenance & Case Quality Issues
  - Authoring & Learning Support

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## Open Questions

- Quality Issues
  - Good vs Bad Cases / Useful vs Redundant Cases
- Controlling Case-Base Growth
  - Building & Maintaining Quality Case-Bases
- Authoring Tools
  - Case-Based Visualization
  - Authoring Guidance
  - Case Discovery – competence holes

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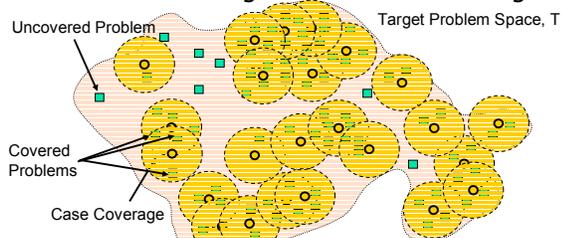
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## Case Competence: The Basics

- Case Coverage & Case-Base Coverage



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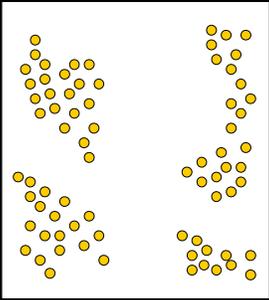
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 **Mapping Case Competence**

- The Top-Level
  - Problem Space
  - Cases & Target Problems
- Case Coverage
  - Competence vs Efficiency
  - The Utility Problem



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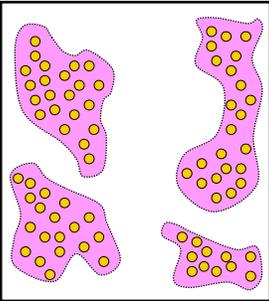
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 **Mapping Case Competence**

- Competence Groups
  - Independent regions of related competence
  - The fundamental unit of competence



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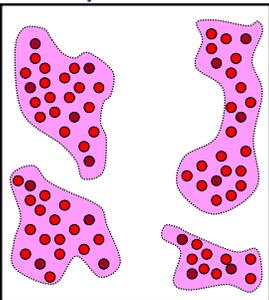
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 **Mapping Case Competence**

- Case Competence
  - Competence categories
- Footprint Cases
  - Cases that provide equivalent coverage to the group as a whole
- Non-Footprint Cases
  - Redundant?



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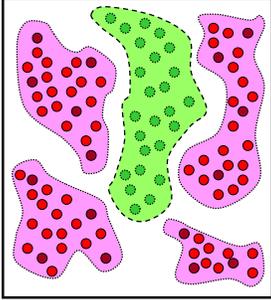
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 **Mapping Case Competence**

- Competence Holes
  - Uncovered regions and problems



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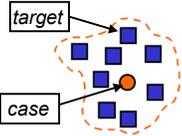
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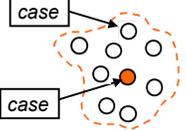
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 The **coverage set** of a **case** is the set of **target** problems that it can solve.

$\text{coverageset}(\bullet) = \{ \blacksquare \text{'s} \}$



... or, by the representativeness assumption ...  
(ie we assume the case-base is representative)



The **coverage set** of a **case** is the set of **cases** that it can solve.

$\text{coverageset}(\bullet) = \{ \circ \text{'s} \}$

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 **Case-Competence: The Basics**

- An *Ideal* Measure of Case Coverage
  - For a case-base CB and a target problem set T
  - $\text{Coverage}(c) = \{ t \in T : \text{Solves}(c,t) \}$
- A *Practical* Measure of Case Coverage
  - CB is a representative sample of T
  - $\text{Coverage}(c) = \{ c' \in \text{CB} : \text{Solves}(c,c') \}$

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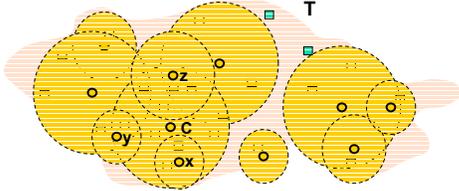
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## Case Competence: The Basics

### ■ Approximating Coverage Sets



$$\text{CoverageSet}(c) = \{ x, y, z \}$$

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## Case Competence: The Basics

### ■ Case-Base Coverage

- How does the coverage of the case-base depend on the coverage of its cases?
- Unique & Redundant Coverage

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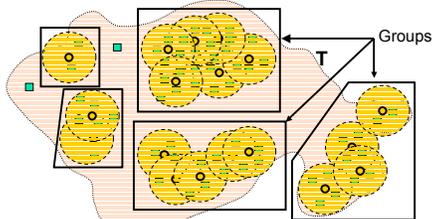
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## A Competence Model

### ■ Competence Groups

- Maximal clusters of cases exhibiting shared coverage.
- "Connectedness" of cases



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## A Competence Model

- Computing Competence Groups
  - $c_1$  &  $c_2$  share coverage iff their case competence overlap
  - $c_1$ ,  $c_2$  &  $c_3$  are a Competence Group iff they share coverage

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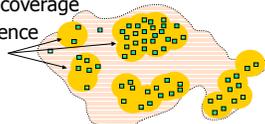
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## A Competence Model

- The Importance of Competence Groups
  - Independent regions of coverage
  - $\Rightarrow$  Independent competence contributions
- Fundamental Unit of Competence ?




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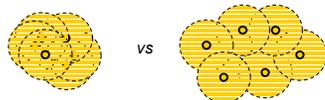
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## A Competence Model

- Group Coverage - The Basic Idea
  - Case Density  $\propto$  Coverage Redundancy  $\propto^{-1}$  Group Coverage



- Regularity Assumption - Similar Problems  $\Rightarrow$  Similar Solutions

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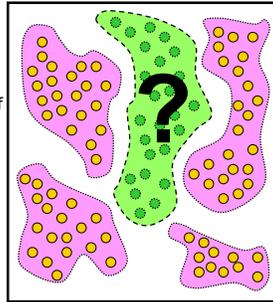
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## What is a Competence Hole?

- What is a competence hole?
  - Any uncovered region of the target space
- What makes a competence hole *interesting*?
  - Size of the hole
  - Relevance to target problems



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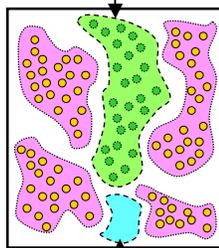
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## Two Types of Competence Holes

**Type 1**  
Insufficient cases within the case-base.  
*Lost coverage.*



**Type 2**  
Due to domain constraints – impossible value combinations.  
*No lost coverage*

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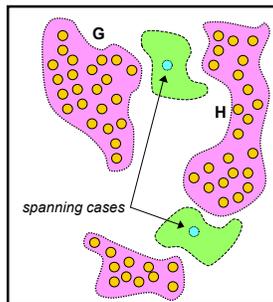
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## Identifying Interesting Holes

- Methodology
  - Competence groups that are close to each other may ultimately merge into a single group
  - The missing cases are competence rich **spanning cases**
- ∴ Search for new spanning cases in the regions between nearby competence groups



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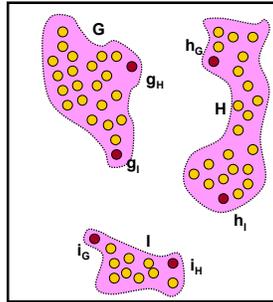
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## Identifying Interesting Holes

- Boundary Cases
  - Each pair of groups **G**, **H** has a corresponding pair of boundary cases,  $g_H$ ,  $h_G$  (●) with maximal similarity
  - ∴ Each group has a set of  $n-1$  boundary cases corresponding to the  $n-1$  other groups in the case-base



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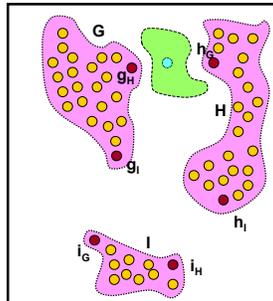
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## Identifying Interesting Holes

- Interesting Holes
  - For each group we can search for new spanning cases between it and its nearest neighbour group.



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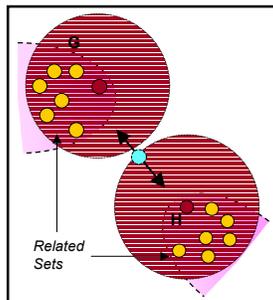
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## Case Generation (Boundary Method)

- Methodology
  - Generate a new case from the feature values of the related sets of the boundary pair cases
- Nominal Features
  - Most frequent value
- Continuous Features
  - Mean value



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## Discussion

- Applications
  - Authoring & Maintenance
- Related Work
  - Competence Categories (Smyth & Keane, IJCAI 1995)
- Assumptions & Applicability
  - Representational Biases

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## Case Authoring

- Current Tools
  - Poor modelling & visualisation techniques
- Authoring Guidance
  - Identification of redundant cases and inefficient groups of cases
  - Identification of regions of poor competence
  - Predictive measures of competence and performance

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## CASCADE

- Case Authoring Support & Development Environment
  - Traditional Authoring Functionality (defining & editing cases)
- Visualisation & Modelling Tools
  - Competence Groups (coverage & density analysis)
  - Competence Graphs

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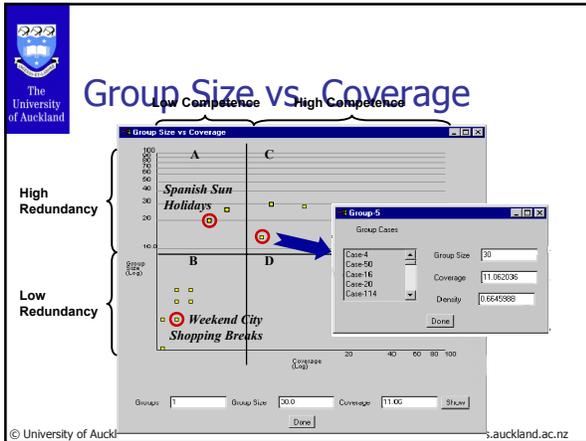
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- ## Related Work
- Competence Categories (*Explanatory Model*)
    - Pivotal, Spanning, Support, Auxiliary Cases
    - Coarse Grained Competence Patterns
  - Current Model (*Predictive Model*)
    - Fine Grained Competence Measures
    - Above categories are found within competence groups. Eg, singleton competence groups hold pivotal cases.

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- ## Assumptions
- Representativeness
    - Case-base is a representative sample of the target problem space  $\Rightarrow$  tractable coverage estimates.
  - Regularity & Uniformity
    - Density models assume that regions of the problem space are regular and uniform.
  - Real World Case-Bases
    - If these assumptions do not hold then the quality of our competence predictions will degrade (gracefully?).

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## Conclusions

- A Competence Model for CBR
  - Positive initial results
- Future Work
  - Further experiments
  - Authoring & maintenance applications
  - Visualising case-bases

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