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Workstation?*

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Abstract

Since a vector supercomputer costs about 2000 times as much as a workstation, it should run programs at least 100 times faster. We discovered that even a 30-fold speedup is optimistic, unless you are willing to invest heavily in code optimization. Furthermore, supercomputers offer inferior floating point precision and, often, no advantage in main memory size. We conclude that few users — mainly cost-insensitive ones — should attempt to port their workstation code to a vector supercomputer. To help you decide if you should port your code, we pose five questions in a self-evaluation format.

When working with a program that is at, or reaching, the acceptable limits of runtime on a workstation, the following question arises naturally: Will the performance of my application increase when run on a supercomputer? In this article, we pose five additional questions to help you answer the original question for yourself. If you answer 'no' to more than one of our questions, it is probably not worthwhile for you to attempt porting your code to a vector supercomputer.

We devote one section of this article to each of our five questions:

1. Would you pay 60 times as much to solve your problem 30 times faster?
2. Can your code be easily vectorized?
3. Will your program be used enough to warrant hand-optimization?
4. Can you afford to retune your software's floating-point arithmetic?
5. Is your application small enough for a supercomputer?

We developed our list of questions to save others from wasting time and energy, as we did, trying to port code from a workstation to a supercomputer.

From 1986 to 1989, we believed we had a application that was well-suited for running on a Cray supercomputer. We were running a series of experiments on a promising new approach for deciding how to route the microscopic wires on a semicustom integrated circuit known as a gate array. Our approach is to generate a fairly large linear program (832 constraints) for a small (12x15) gate array. The solution of the linear program indicates how wires might be placed into the Manhattan-like channels between the gates in the array [11].

Until February 1990, the cpu-intensive kernel of our wire-routing system was Roy E. Marsten's XMP package for solving linear programs. This package of FORTRAN routines is running on many different computers, ranging from PCs to supercomputers [8, page 3]. Recently, for the reasons outlined below, we replaced the XMP linear program solver with a new package called CPLEX [2].

Since our Sun-3 workstation took 100 seconds to solve our 832-constraint problem using the XMP library, we feared that our system would not be feasible for large gate arrays. To give you a sense of scale, a modern gate array such as the 1 μ m CMOS TGC118 has 18,620 sites in a 133x140 array [12]. Routing such a large array with our method would result in a linear program approximately 100 times larger than our 12x15 example. Since linear programming by the simplex method (as in XMP and CPLEX) usually runs in $O(n^3)$ time, Sun-3 runtime on a 133x140 array would be roughly $(100)^3$ times as long as in our 12x15 example — perhaps 10^8 seconds, or about two years.

Since the Cray-2 typically runs at tens of MFLOPS, and our Sun-3 with a 68881 co-processor typically runs at tens of KFLOPS, we naively hoped to see our runtime decrease by a factor of 1000 after porting our program to a Cray-2. With the expected 1000-fold speedup, we could route a full TGC118 array in a day of Cray-2 runtime.

In retrospect, our expectation of a 1000-fold speedup was naive. On our code, we observed only a 20-fold speedup: a Cray-2 took 5 seconds to solve our 832-constraint benchmark, as opposed to 100 seconds on a Sun-3.

After modernizing both software and hardware early in 1990, we still see no reason to run our application on a supercomputer. Our new Sun-4 runs about 2.5 times faster than our old Sun-3, on the XMP code. We gain an additional factor of 15 by replacing the XMP code with the CPLEX linear program solver. With CPLEX, our Sun-4 workstation solves our 832-constraint benchmark in 2.5 seconds, a 40-fold improvement on our Sun-3 runtime with XMP. Using the $O(n^3)$ runtime extrapolation described above, we might now be able to route the wires on a 133×140 gate array in two or three weeks of Sun-4 runtime. This is exciting, because we are now within a factor of four or so of economic feasibility for our wire-routing system.

It would be interesting for us to use the CPLEX code to solve our 832-constraint problem on a Cray, in order to complete the comparison. Unfortunately, our \$500 CPLEX license covers only the Sun-4. According to CPLEX promotional literature, however, their code runs only 10 to 14 times faster on a Cray Y-MP than on a Sun-4, for five standard linear programming problems of 1,554 to 16,170 constraints. We would expect to see a similar 10- to 14-fold speedup on our 832-constraint problem.

In summary, neither our old or new experiments showed more than a 20-fold speed advantage in moving our programs to a Cray. This small improvement does not justify either the cost of the port or the relative expense of access to the Cray. Although we get our Cray cycles "for free" (via a straightforward grant-writing process), we are interested in proving the economic feasibility of our wire-routing method. Thus we view the 100-fold increase in actual cost of rapidly solving a wire-routing problem on a Cray, versus solving it 20 times more slowly on a workstation, as a deciding factor in our comparison.

The discussion above has centered on speedup and cost ratios. These are important, but by no means the sole factors in considering whether to port code to a supercomputer. Below, we treat other important issues, in addition to speedup, in our five-question framework for deciding "to port or not to port?"

1. Would you pay 60 times as much to solve your problem 30 times faster?

We obtained only a 10- to 20-fold speedup when we moved our workstation code to a Cray. Your code may be more amenable to speedup than ours. Still, we doubt you will see as much as a 30-fold speedup, without an expensive and time-consuming recoding. In the following section, we argue for a 30-fold limit on speedups; if you accept this value for now, we can make some broad-brush economic arguments.

A vector supercomputer costs between ten and twenty million dollars. A workstation costs between five and ten thousand dollars. This 2000-fold difference in purchase cost can be translated into a 2000-fold difference in operating cost, if one assumes that yearly operating costs are 30% to 50% of the purchase cost. Both workstations and supercomputers are functionally obsolete within five years, so that yearly depreciation and finance charges alone are 20% to 30% of the purchase cost. Yearly budgets for operating personnel, software, and hardware maintenance each add another 5% to 10% of the hardware purchase cost to the yearly operating expense. Thus a supercomputer costs about \$1000 per hour to operate, and a workstation costs about 2000 times less, or about \$10 per day.

If you obtain a 30-fold speedup by using a supercomputer instead of a workstation, then you will pay $2000 \div 30 = 66.7$ times as much to solve each problem. In some applications, this is perfectly acceptable. Consider the problem of weather prediction. If you developed a code that enables a Sun workstation to predict tomorrow's weather in just 24 hours of runtime, your code would have no commercial value. However, if your code ran in just 1 hour on a Cray, you could sell your weather predictions for a tidy profit, even after paying \$1000 per prediction for your Cray runtime.

Our advice, then, is for you to examine your the time-value of results in your application, to see if you are able to accept a 30-fold speedup at a 60-fold increase in cost.

In our case, we are not able to justify the increased cost of a Cray computation. We believe that our end-user population would not be willing to spend more than about \$1000 for a solution to a wire-routing problem, nor would they be willing to wait more than a week for the results. One week of Sun-4 time will solve about 18 times as many problems as one thousand dollars (one hour) of Cray time, even assuming an optimistic 20-fold speedup for our application.

2. Can your code be easily vectorized?

By following the advice in this section, you should be able to determine if you would obtain more than a 30-fold speedup if you moved your workstation code to a supercomputer.

In a nutshell, the difficulty with using a supercomputer efficiently is that code written for use on scalar machines, such as a workstation or a mainframe, will not take full advantage of the specialized functional units of a supercomputer. To gain the potential 100- to 1000-fold speed advantage of a vector supercomputer, programs must be vectorized [7, page 81]. This can be accomplished in two ways.

The simplest approach is to compile your unmodified source code on a supercomputer's vectorizing compiler. The second, and much more expensive, method of vectorization is to employ a skilled programmer to rewrite portions of the source code. We discuss the use of vectorizing compilers in this section, deferring code restructuring to the next section.

Despite major advances in compiler technology, any of the following programming constructs hamper the vectorization of loops: recursion, subroutine calls, I/O statements, assigned GOTO's, certain nested if statements, GOTO's that exit the loop, backward transfers within the loop, and references to non-vectorized external functions [7, page 90]. Such constructs are common but relatively innocuous, outside of inner loops. When they appear in an inner loop, however, that loop will not be vectorizable.

Code that is not vectorizable will not run much faster on a supercomputer than on a workstation. Modern workstations execute about 10 million instructions per second. Vector supercomputers run at about the same speed whenever the operands and the machine instructions cannot be prefetched. In either case, the limiting factor is the 100 nanoseconds or so it takes to fetch an arbitrary operand from semiconductor memory (RAM).

Even when a supercomputer's compiler is successful at vectorizing an inner loop, loops that are iterated only a small number of times will not be accelerated appreciably: they may even run more slowly when executed in vector mode!

A final warning: if your workstation spends less than 80% of its time executing your code's inner loops, you will not see a large speedup if you move this code to a supercomputer. This prediction is based on classic work by G. Amdahl[1]; here is a brief explanation of how Amdahl's Law applies in this scenario. The code outside your inner loops is unlikely to be accelerated much, due to its use of non-vectorizable constructs. Even if this code were accelerated by a factor of six, and even if your inner loops were executed instantaneously, your total speedup can be no more than $6/(20\%) = 30$, if 20% of your workstation runtime is due to non-inner loop computations.

If you are able to identify the inner loop of your source code, you may be able to estimate its speedup. The idea is to find speedup data for a similar loop, in a book[7] or some other published source[5, 9]. The iteration count of the loop is a critical parameter[6]. We present some illustrative data below.

On a Cray Y-MP in single processor mode, the three loops A, B and C all run at about 5 MFLOPS when the iteration count n is 10, at 33 to 60 MFLOPS when $n = 100$, and at 33 to 220 MFLOPS when $n = 1000$. Loops A and B are therefore amenable to vectorization, running in excess of 100 MFLOPS when $n > 100$. Loop C's indirect addressing limits it to 33 MFLOPS, even for large n .

```
Loop A:      do 1 i=1,n
              1  s=s+a(i)*b(i)
Loop B:      do 2 i=2,n
              do 2 j=1,i-1
              2  a(i)=a(i)+b(i,j)*a(i-j)
Loop C:      do 3 i=1,n
              3  a(ia(i)) = b(ia(i)) + c(ia(i))
```

By way of contrast, all three loops run at 1 to 3 MFLOPS on a Sun-4 workstation, for any $n > 2$.

Summarizing our discussion of speedup analysis, we assert that unless you have simple arithmetic statements in your inner loops, unless your vector lengths are longer than 100, unless you have no indirect addressing in your inner loops, and unless your inner loops account for the vast majority of your program execution time, you surely will not observe a speedup greater than 30 when moving from a workstation to a supercomputer.

You may be uninterested in learning enough about vectorizing compilers to estimate the speedup possible on your code. As a simpler alternative, we suggest you merely compile your code on a supercomputer, then run it on a representative set of test data. Most supercomputer centers are willing to let a potential client make a test run of this form, with little bureaucratic overhead.

We made a test run on several different workstations and supercomputers, timing how long each takes to solve our 832-constraint linear program with the XMP code. Here are our results. A Cray X-MP achieved

- a 30-fold speedup over a Sun-3,
- a 12-fold speedup over a Sun-4,
- a 6-fold speedup over a DECstation 3100, and
- a 1.5-fold speedup over a Cray-2.

The actual runtimes were

- 101 seconds on our Sun-3/160,
- 42.1 seconds on our Sun-4/110,
- 19.9 seconds on a DECstation 3100,
- 5.1 seconds on a Cray-2, and
- 3.4 seconds on a Cray X-MP.*

Leaving the obsolescent Sun-3 out of the comparison, the largest speedup observed when moving from a workstation to a Cray is 12. Thus, the \$10-per-day workstations will solve the same set of problems about 200 times more cheaply than a \$1000-per-hour supercomputer, albeit 10 times more slowly.

We made more than a dozen runs on the Cray-2, trying all combinations of the compiler flags that affect vectorization. None had a significant effect on the runtime of the XMP source code, for our test data. This implies that the code is not vectorizable. Upon further investigation, we found that the inner loop of the XMP code iterates, on average, just 1.8 times per entry. This is sufficient explanation for its non-vectorizability.

As mentioned in the introduction, we recently switched to a better linear program solver, CPLEX. It is superior not only in runtime, but in the number of iterations and in the number of integers in its solution vector.

When we mounted CPLEX on the Sun-4, we found it could solve our 832-constraint problem in just 2.5 seconds. This is twice as fast as the Cray-2 running the inferior XMP linear program package! Unfortunately, a license to run CPLEX on a supercomputer is very expensive, so we are unable to directly measure its speedup, on our problems, on a supercomputer. However, according to its supplier's data, CPLEX runs only 10 to 14 times faster on a Cray Y-MP than it does on a Sun-4, indicating that CPLEX, like XMP, is not effectively vectorizable.

We note, in passing, that the next generation of workstations will have vectorized floating point units. Already, one can buy a floating-point accelerator board for a Sun workstation, boosting its peak performance to 80

*All workstations had floating point chips and at least 8 MBytes of memory. The Sun-3/160 is rated at 2 MIPS; it was running Sun UNIX 4.2 release 3.5. The Sun-4/110 is rated at 7 MIPS; it was running SunOS Unix 4.0. The DECstation 3100 is rated at 14 MIPS; it was running an early version of its operating system, ULTRIX-32 ver 2.0 rev 7.0. The Cray-2 is rated at 1800 MFLOPS (peak); it has 4 processors and 512 MWords of memory; it was running UNICOS 4.0 at the time of our experiments. The Cray X-MP has 4 processors, 16 MWords of primary memory, and 128 MWords of semiconductor secondary memory; it was running UNICOS 5.0. We used the CFT77 compiler on the Crays, and the FORTRAN-77 compiler supplied by each workstation's manufacturer.

MFLOPS. This development will greatly reduce the maximum speedups observed when moving from a workstation to a supercomputer. Paradoxically, it may also expand the use of supercomputers, since code optimized for a vectorized workstation will probably run efficiently on a supercomputer.

3. Will your program be used enough to warrant hand-optimization?

As noted in the preceding section, global compiler directives are not often sufficient to give much (if any) speedup. Hand-optimization is necessary for efficient use of the functional units of a supercomputer, in order to approach its full speed advantage over a scalar processor.

The time required to hand-optimize a program will depend upon the size of the utilized code [7, pages 6–7], the style in which it was written, and the programmer's familiarity with it. By style we mean, "Does the program contain good comments and descriptive variables?"

Of course, the expense of programmer-mediated optimization must be offset with the savings gained from the decrease in execution time. In the worst case, it will take months or years to hire and train programmers to rewrite, document, and test a few thousand lines of code. In the best case, one's supercomputer center consultants may be able to point out a simple modification to your inner loop, achieving a factor-of-ten speedup in a matter of days.

In our case, examination of the XMP source code showed its inner loop to be a prime example of "dusty deck" FORTRAN. Effective vectorization is infeasible, since the entire XMP program is built around a data structure (a row-oriented sparse matrix) that will not support vectorization in matrices, like ours, with only a few non-zeros per row. If we completely restructured the program, storing our matrix by blocks or by sparse diagonals [4], we might do better, but this would take tens of programmer-years. We are not skilled in such work, and we know of three linear-programming development projects in progress at other sites right now.

A final bit of advice: before rewriting your own code, we strongly recommend you make a thorough search for similar code that has already been vectorized. Should this search be successful, you stand to save a lot of time, money, and aggravation.

4. Can you afford to retune your software's floating-point arithmetic?

Our fourth question is pointed at the profound differences between, and general inferiority of, floating-point arithmetic on a Cray versus that on a workstation. All modern workstations follow the IEEE 754 floating-point standard. Supercomputers do not.

In general, you should expect to encounter little difficulty when porting your code from one IEEE-standard workstation to another. If, however, your code is at all sensitive to floating-point roundoff errors, you should be prepared to "retune" and revalidate your code upon moving it to a supercomputer.

The Cray floating point storage format has 1 sign bit, 15 exponent bits, and 48 mantissa bits. Floating point numbers have the most significant bit in the leftmost mantissa bit, giving 48 bits of precision [3]. The IEEE-standard double-precision storage format has 1 sign bit, 11 exponent bits, and 52 mantissa bits. Here, the most significant bit is implied, giving the user 53 bits of precision [10, page 1-9], fully 5 bits more storage precision than is available on the Cray-2. Furthermore, the IEEE standard specifies a roundoff algorithm to be employed when storing a floating-point number; Crays do some form of truncation.

The Cray multiplication algorithm uses 56 bits of precision [3]. This is significantly less than the intermediate format of the IEEE standard, which has 64 bits of precision [10, page 1-9]. The 56-bit Cray result is not an intermediate format in the IEEE sense, since it is not available after the multiplication is complete. Thus, for example, inner-product accumulations are done with at most 48 bits of precision on the Cray, whereas the IEEE standard provides 64 bits.

In computations where precision is not crucial, workstation users may employ the single-precision IEEE-standard floating point storage format. In this format, a floating point number occupies only 32 bits of storage, but its range and precision are limited. Computations on single-precision numbers proceed at about the same speed as double-precision numbers, unless bandwidth to and from workstation memory is a bottleneck.

We note, in passing, that very-high-precision floating point arithmetic is available on some workstations (such as the DECStation 3100) and the Cray supercomputers, for users willing to pay a substantial time penalty. It takes four to ten times as long to run a program with about 100 bits of precision, as opposed to the 48- to 64-bit precision of the standard floating point arithmetic.

In summary, although there is a slight time penalty for *storing* a floating point number in double precision on a workstation, floating point arithmetic

on a workstation is always *performed* at a higher level of precision than on a Cray.

In addition to the precision advantage outlined above, the IEEE standard provides a straightforward method for handling exceptional operations, such as dividing by 0 or taking the square root of a negative number. These exceptional operations yield results that, when printed, are easily understood. The alternative method of handling exceptions, seen on Crays (and on older mainframes) is an easily-lost or misinterpreted error message, or, possibly, an abnormal termination of your job. The latter is irritating, to say the least, when the exceptional operation would not have affected the major results of your run.

In our application, we observed that the XMP linear program package was unable to solve a 1500-constraint problem when it was compiled and run on a Cray-2. The identical XMP source code was able to solve this problem when compiled and run on the Sun-3, the Sun-4, and the DECstation 3100. We surmise that the loop termination conditions in the XMP package were tuned for IEEE-standard arithmetic, and would require some modification to work adequately on the Cray-2. If we were still interested in porting XMP to a Cray, we would contact its supplier for advice on modifying the code.

We conclude that the peculiarities and relative imprecision of supercomputer floating-point arithmetic could pose severe difficulties when porting code from a workstation to a supercomputer.

5. Is your application small enough for a super-computer?

Most people would assume that a supercomputer can handle much larger programs and datasets than would fit on a workstation. Indeed, this was true in the recent past, but the differences in memory size between supercomputers and workstations is generally small, and decreasing rapidly.

The Cray-2 is the only member of the Cray line that can be configured with thousands of megabytes of primary memory. By contrast, it is a rare workstation or modern supercomputer that has more than a few tens of megabytes. If you need more main memory than this, you probably belong on a mainframe.

The importance of matching application size to primary memory space can not be overstated. If your program frequently accesses a data structure that is larger than its main memory, its runtime will be limited by your computer's disk transfer time. A slowdown for this reason is called "disk thrashing." In the worst case, your program might make random accesses of single words in a data structure stored on its disk. If this occurs, your workstation could run 100,000 times more slowly than if its data structure

fit into its primary memory: a random access to fast semiconductor RAM takes about 100 nanoseconds, while a random access to a fast disk takes about 10 milliseconds.

On a supercomputer, disk thrashing has more severe economic consequences than it does on a workstation. A \$1,000-per-hour Cray Y-MP can do only a few more disk accesses per second than can a \$10-per-day workstation. Also, the cost of a disk access on a workstation can be mitigated by multiprogramming, a technique whereby another task (or another user) can use the workstation's CPU(s) while the first task is awaiting disk service. It takes only a millisecond or two to switch tasks. By contrast, a multiprogrammed Cray processor also takes a millisecond or two to switch tasks — but this millisecond of “wasted CPU time” costs 2000 times as much as on a workstation!

Note that the Cray X-MP and Y-MP architectures include a large semiconductor “secondary memory” designed to allow rapid block-level accesses to a 1000-megabyte dataset. There is thus some hope of efficiently running large programs on these machines. Still, we believe that any application which is too big to fit on a workstation belongs on a mainframe or a Cray-2. If it is too big to fit on these, it belongs on a workstation, because an inexpensive CPU can keep its disks busy much more cost-effectively than can a Cray.

In order to estimate your program's space requirements, we suggest asking your computation center's consulting staff for help. If you give them a copy of your code and a sample dataset, they should be able to measure (or tell you how to measure) your program's use of the system's disk drives and virtual memory. A bit of analysis and examination of source code documentation will be in order as well, in order to extrapolate how your program would behave on a worst-case set of input data.

Alternatively, you might try to calculate the maximum total size of your program's data and code area. You can then use this as a worst-case estimate of your program's memory requirements. Most programs will not thrash if limited to a small fraction of their total memory area, since at any given time, they will access only a small part of their data and code. The actively-referenced part of a program's data and code space is called its “working set.”

In our application, a linear program with 1000 constraints uses 0.5 MBytes of memory for data storage on the workstations, or 0.7 MBytes of memory on the Cray-2. The difference between the Cray-2 and the workstation is a result of the use of 4-byte integers on the workstations, as opposed to the 8-byte Cray-2 integers. On both machines, the space required for the linear program solution code space quickly becomes irrelevant as the problem size increases.

Since we are using linear programming code based on sparse matrices, our working set will grow with the number of non-zeros in the constraint matrix. In our problems, we expect the number of non-zeros per row to be essentially independent of the number of constraints. We thus extrapolate linearly, finding that 40 MBytes of working set should be enough to handle the 80,000-constraint linear program arising from using our method to route the wires in a modern gate array. Thus a memory-rich workstation, or for that matter, a Cray X-MP or Y-MP, should be able to solve a wire routing problem for even the largest current gate arrays. Gate arrays are expected to become larger in the future, but so are workstation memories.

We conclude that our program's working set is small enough to fit on any supercomputer or well-configured workstation.

6. Summary

We have posed five questions to help you decide whether or not to port your application to a supercomputer:

1. Would you pay 60 times as much to solve your problem 30 times faster?
2. Can your code be easily vectorized?
3. Will your program be used enough to warrant hand-optimization?
4. Can you afford to retune your software's floating-point arithmetic?
5. Is your application small enough for a supercomputer?

If you answer "no" to the first question, but you think you could obtain a speedup greater than 30 with a vectorizing compiler alone (question two), or with hand-optimization followed by vectorized compilation (question three), then porting your code may well make economic sense. A negative answer to either question four or five, however, is a sure indication of trouble. Simplifying, we thus assert that if you answer any two of our questions "no," your application does not belong on a supercomputer.

Our application scored four "no" answers: in hindsight, it is strange that we ever considered porting our sparse linear-programming code to a supercomputer!

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