COMPSCI 320SC 2014 Midterm Test

Attempt all questions. (Use of calculators is NOT permitted.)

Put the answers in the space below the questions. Write clearly and $show\ all\ your\ work!$

Marks for each question are shown below and just before each answer area.

This 50 minute test is worth 10% of your final grade for the course.

Question #:	1	2	3	4	Total
Possible marks:	5	5	5	5	20
Awarded marks:					

University ID:	
Student Name:	
Student Signature:	
Time Finished:	
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- 1. Recall Huffman's greedy algorithm for constructing an optimal prefix code. Consider the behavior of this algorithm on the sample instance with characters $\{a,e,i,o,u\}$ and frequencies $f_a=.32$, $f_e=.25, f_i=.20, f_o=.18$ and $f_u=.05$.
 - (a) Draw the Huffman prefix tree for this instance.

(3 marks)

(b) What is the average number of bits per letter (ABL) for this code?

(2 marks)

3

2. Consider the following divide-and-conquer "algorithm":

```
function printer(int n)

if n == 0 return

for j = 1 to 3 do

printline "hello world"

printer(\lfloor n/3 \rfloor)
```

Let T(n) denote the number of lines of output generated by a call of printer(n).

(a) Provide a recurrence equation for T(n).

(2 marks)

(b) Solve the recurrence exactly for n being a power of 3 (that is, $n = 3^k$ for integer $k \ge 0$). (3 marks)

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- 3. Suppose you are given an edge-weighted connected graph G of order n and size $m \le n + 10$. You may assume all the edge weights are distinct. Note that for any cycle C in the graph G we know the largest edge weight of C is not used in *some* minimum spanning tree.
 - (a) Give a greedy algorithm that finds a minimum spanning tree in time O(n). (3 marks)

(b) Explain why the algorithm you gave in part (a) is correct and that its running time is linear. (2 marks)

(1 mark)

(1 mark)

(d) If the Perrin number P(n) is divisible by n then n is a prime number.

(e) The complex number $e^{\pi i} = -1$.