<u>CS 367</u>

Artificial Intelligence

Part II: Search & Planning

Semester 2 - 2007

Contact Info

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Course Info for Part II

Assignment 2:

Available on web: 20 August Due: 24 September

Topics:

- Problem Solving and Search
- Search Algorithms
 - Uninformed Search Algorithms
 - Informed Search Algorithms

• Planning

Totally-Ordered Plans Partially-Ordered Plans

PROBLEM SOLVING AND SEARCH

Chapter 3, Sections 1–5

Outline

- \Diamond Problem-solving agents
- \diamond Problem types
- \diamond Problem formulation
- \diamond Example problems
- \diamond Basic search algorithms

Problem-solving agents

Restricted form of general agent:

```
function SIMPLE-PROBLEM-SOLVING-AGENT( percept) returns an action
   static: seq, an action sequence, initially empty
            state, some description of the current world state
            qoal, a goal, initially null
            problem, a problem formulation
   state \leftarrow \text{UPDATE-STATE}(state, percept)
   if seq is empty then
        goal \leftarrow FORMULATE-GOAL(state)
        problem \leftarrow FORMULATE-PROBLEM(state, goal)
        seq \leftarrow SEARCH(problem)
   action \leftarrow \text{Recommendation}(seq, state)
   seq \leftarrow \text{REMAINDER}(seq, state)
   return action
```

Note: this is *offline* problem solving; solution executed "eyes closed." *Online* problem solving involves acting without complete knowledge.

Part II: Lecture 1

Example: Romania

On holiday in Romania; currently in Arad. Flight leaves tomorrow from Bucharest

Formulate goal:

be in Bucharest

Formulate problem:

states: various cities *actions*: drive between cities

Find solution:

sequence of cities, e.g., Arad, Sibiu, Fagaras, Bucharest



Problem types

Deterministic, fully observable \implies single-state problem Agent knows exactly which state it will be in; solution is a sequence

Non-observable \implies conformant problem

Agent may have no idea where it is; solution (if any) is a sequence

Nondeterministic and/or partially observable ⇒ *contingency problem* percepts provide *new* information about current state solution is a *tree* or *policy* often *interleave* search, execution

Unknown state space \implies *exploration problem* ("online")

Single-state, start in #5. <u>Solution</u>??



Single-state, start in #5. Solution?? [*Right*, Suck]

Conformant, start in $\{1, 2, 3, 4, 5, 6, 7, 8\}$ e.g., *Right* goes to $\{2, 4, 6, 8\}$. Solution??



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Contingency, start in #5 Murphy's Law: *Suck* can dirty a clean carpet Local sensing: dirt, location only. <u>Solution</u>??



Single-state, start in #5. Solution?? [Right, Suck]

Conformant, start in $\{1, 2, 3, 4, 5, 6, 7, 8\}$ e.g., *Right* goes to $\{2, 4, 6, 8\}$. <u>Solution</u>?? [*Right*, *Suck*, *Left*, *Suck*]

Contingency, start in #5 Murphy's Law: *Suck* can dirty a clean carpet Local sensing: dirt, location only. Solution??

[Right, if dirt then Suck]



Single-state problem formulation

A *problem* is defined by four items:

initial state e.g., "at Arad"

successor function S(x) = set of action-state pairse.g., $S(Arad) = \{\langle Arad \rightarrow Zerind, Zerind \rangle, \ldots \}$

goal test, can be explicit, e.g., x = "at Bucharest" implicit, e.g., NoDirt(x)

path cost (additive) e.g., sum of distances, number of actions executed, etc. c(x, a, y) is the step cost, assumed to be ≥ 0

A *solution* is a sequence of actions leading from the initial state to a goal state

Selecting a state space

Real world is absurdly complex

 \Rightarrow state space must be *abstracted* for problem solving

(Abstract) state = set of real states

(Abstract) action = complex combination of real actions
 e.g., "Arad → Zerind" represents a complex set
 of possible routes, detours, rest stops, etc.
For guaranteed realizability, any real state "in Arad"
 must get to *some* real state "in Zerind"

(Abstract) solution =

set of real paths that are solutions in the real world

Each abstract action should be "easier" than the original problem!

Example: vacuum world state space graph



<u>states</u>?? <u>actions</u>?? <u>goal test</u>?? path cost??

Example: vacuum world state space graph



states??: integer dirt and robot locations (ignore dirt amounts)
actions??: Left, Right, Suck, NoOp
goal test??: no dirt
path cost??: 1 per action (0 for NoOp)



Start State

Goal State

states?? actions?? goal test?? path cost??



states??: integer locations of tiles (ignore intermediate positions)
actions??: move blank left, right, up, down (ignore unjamming etc.)
goal test??: = goal state (given)
path cost??: 1 per move

[Note: optimal solution of *n*-Puzzle family is NP-hard]

Example: robotic assembly



states??: real-valued coordinates of robot joint angles parts of the object to be assembled

<u>actions</u>??: continuous motions of robot joints

goal test??: complete assembly with no robot included!

path cost??: time to execute

Tree search algorithms

Basic idea:

offline, simulated exploration of state space by generating successors of already-explored states (a.k.a. *expanding* states)

function TREE-SEARCH(problem, strategy) returns a solution, or failure
initialize the search tree using the initial state of problem
loop do
 if there are no candidates for expansion then return failure
 choose a leaf node for expansion according to strategy
 if the node contains a goal state then return the corresponding solution
 else expand the node and add the resulting nodes to the search tree
end



Tree search example



Tree search example



Implementation: states vs. nodes



The Expand function creates new nodes, filling in the various fields and using the SUCCESSORFN of the problem to create the corresponding states.

Implementation: general tree search

```
function TREE-SEARCH(problem, fringe) returns a solution, or failure
   fringe \leftarrow \text{INSERT}(\text{MAKE-NODE}(\text{INITIAL-STATE}[problem]), fringe)
   loop do
       if fringe is empty then return failure
       node \leftarrow \text{REMOVE-FRONT}(fringe)
       if GOAL-TEST[problem] applied to STATE(node) succeeds return node
       function EXPAND( node, problem) returns a set of nodes
   successors \leftarrow \text{the empty set}
   for each action, result in SUCCESSOR-FN[problem](STATE[node]) do
        s \leftarrow a \text{ new NODE}
        PARENT-NODE[s] \leftarrow node; ACTION[s] \leftarrow action; STATE[s] \leftarrow result
        PATH-COST[s] \leftarrow PATH-COST[node] + STEP-COST(node, action, s)
        \text{DEPTH}[s] \leftarrow \text{DEPTH}[node] + 1
        add s to successors
   return successors
```

Search strategies

A strategy is defined by picking the order of node expansion

Strategies are evaluated along the following dimensions: completeness—does it always find a solution if one exists? time complexity—number of nodes generated/expanded space complexity—maximum number of nodes in memory optimality—does it always find a least-cost solution?

Time and space complexity are measured in terms of b—maximum branching factor of the search tree d—depth of the least-cost solution m—maximum depth of the state space (may be ∞)

Uninformed search strategies

Uninformed strategies use only the information available in the problem definition

Breadth-first search

Uniform-cost search

Depth-first search

Depth-limited search

Iterative deepening search

Expand shallowest unexpanded node



Expand shallowest unexpanded node



Expand shallowest unexpanded node



Expand shallowest unexpanded node



Complete??

Complete?? Yes (if *b* is finite)

Time??

Complete?? Yes (if *b* is finite)

<u>Time</u>?? $1 + b + b^2 + b^3 + \ldots + b^d + b(b^d - 1) = O(b^{d+1})$, i.e., exp. in d Space??

Complete?? Yes (if *b* is finite)

<u>Time</u>?? $1 + b + b^2 + b^3 + \ldots + b^d + b(b^d - 1) = O(b^{d+1})$, i.e., exp. in d

<u>Space</u>?? $O(b^{d+1})$ (keeps every node in memory)

Optimal??
Complete?? Yes (if *b* is finite)

<u>Time</u>?? $1 + b + b^2 + b^3 + \ldots + b^d + b(b^d - 1) = O(b^{d+1})$, i.e., exp. in d

<u>Space</u>?? $O(b^{d+1})$ (keeps every node in memory)

Optimal?? Yes (if cost = 1 per step); not optimal in general

Space is the big problem; can easily generate nodes at 10MB/sec so 24hrs = 860GB.

Uniform-cost search

Expand least-cost unexpanded node

Implementation:

fringe = queue ordered by path cost

Equivalent to breadth-first if step costs all equal

<u>Complete</u>?? Yes, if step cost $\geq \epsilon$

<u>Time</u>?? # of nodes with $g \leq \text{ cost of optimal solution}$, $O(b^{\lceil C^*/\epsilon \rceil})$ where C^* is the cost of the optimal solution

Space?? # of nodes with $g \leq \text{ cost of optimal solution, } O(b^{\lceil C^*/\epsilon \rceil})$

Optimal?? Yes—nodes expanded in increasing order of g(n)

Expand deepest unexpanded node



Expand deepest unexpanded node



Expand deepest unexpanded node



Expand deepest unexpanded node



Expand deepest unexpanded node



Expand deepest unexpanded node



Expand deepest unexpanded node



Expand deepest unexpanded node



Expand deepest unexpanded node



Expand deepest unexpanded node

Implementation:

fringe = LIFO queue, i.e., put successors at front

Expand deepest unexpanded node

Implementation:

fringe = LIFO queue, i.e., put successors at front



Expand deepest unexpanded node

Implementation:

fringe = LIFO queue, i.e., put successors at front



Complete??

<u>Complete</u>?? No: fails in infinite-depth spaces, spaces with loops Modify to avoid repeated states along path ⇒ complete in finite spaces

Time??

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<u>Time</u>?? $O(b^m)$: terrible if m is much larger than dbut if solutions are dense, may be much faster than breadth-first

Space??

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<u>Time</u>?? $O(b^m)$: terrible if m is much larger than dbut if solutions are dense, may be much faster than breadth-first

<u>Space</u>?? O(bm), i.e., linear space!

Optimal??

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<u>Time</u>?? $O(b^m)$: terrible if m is much larger than dbut if solutions are dense, may be much faster than breadth-first

<u>Space</u>?? O(bm), i.e., linear space!

Optimal?? No

Depth-limited search

= depth-first search with depth limit l,

i.e., nodes at depth l have no successors

Recursive implementation:

```
function DEPTH-LIMITED-SEARCH( problem, limit) returns soln/fail/cutoff
RECURSIVE-DLS(MAKE-NODE(INITIAL-STATE[problem]), problem, limit)
function RECURSIVE-DLS(node, problem, limit) returns soln/fail/cutoff
cutoff-occurred? \leftarrow false
if GOAL-TEST[problem](STATE[node]) then return node
else if DEPTH[node] = limit then return cutoff
else for each successor in EXPAND(node, problem) do
result \leftarrow RECURSIVE-DLS(successor, problem, limit)
if result = cutoff then cutoff-occurred? \leftarrow true
else if result \neq failure then return result
if cutoff-occurred? then return cutoff else return failure
```

Iterative deepening search

```
function ITERATIVE-DEEPENING-SEARCH(pr_{oblem}) returns a solution

inputs: problem, a problem

for depth \leftarrow 0 to \infty do

result \leftarrow DEPTH-LIMITED-SEARCH(problem, depth)

if result \neq cutoff then return result

end
```

Iterative deepening search l = 0



►(A)







Iterative deepening search l = 3



Complete??

Complete?? Yes

Time??

Complete?? Yes

Time??
$$(d+1)b^0 + db^1 + (d-1)b^2 + \ldots + b^d = O(b^d)$$

Space??

Complete?? Yes

Time??
$$(d+1)b^0 + db^1 + (d-1)b^2 + \ldots + b^d = O(b^d)$$

 $\underline{Space}?? O(bd)$ $\underline{Optimal}??$

Complete?? Yes

Time??
$$(d+1)b^0 + db^1 + (d-1)b^2 + \ldots + b^d = O(b^d)$$

Space?? O(bd)

Optimal?? Yes, if step cost = 1

Can be modified to explore uniform-cost tree

Numerical comparison for b = 10 and d = 5, solution at far right:

 $N(\mathsf{IDS}) = 50 + 400 + 3,000 + 20,000 + 100,000 = 123,450$ $N(\mathsf{BFS}) = 10 + 100 + 1,000 + 10,000 + 100,000 + 999,990 = 1,111,100$

Summary of algorithms

Criterion	Breadth- First	Uniform- Cost	Depth- First	Depth- Limited	lterative Deepening
Complete?	Yes*	Yes*	No	Yes, if $l \geq d$	Yes
Time	b^{d+1}	$b^{\lceil C^*/\epsilon \rceil}$	b^m	b^l	b^d
Space	b^{d+1}	$b^{\lceil C^*/\epsilon \rceil}$	bm	bl	bd
Optimal?	Yes*	Yes*	No	No	Yes

Repeated states

Failure to detect repeated states can turn a linear problem into an exponential one!



Graph search

```
function GRAPH-SEARCH( problem, fringe) returns a solution, or failure

closed \leftarrow an empty set

fringe \leftarrow INSERT(MAKE-NODE(INITIAL-STATE[problem]), fringe)

loop do

if fringe is empty then return failure

node \leftarrow REMOVE-FRONT(fringe)

if GOAL-TEST[problem](STATE[node]) then return node

if STATE[node] is not in closed then

add STATE[node] to closed

fringe \leftarrow INSERTALL(EXPAND(node, problem), fringe)

end
```

Summary

Problem formulation usually requires abstracting away real-world details to define a state space that can feasibly be explored

Variety of uninformed search strategies

Iterative deepening search uses only linear space and not much more time than other uninformed algorithms