

COMPSCI 210 S1T 2007 Tutorial One

Transformation of the number:

1. Transforms binary, octal, and hexadecimal to **decimal**

110011 (base 2) is:

$$110011_2 = 1 \times 2^{**5} + 1 \times 2^{**4} + 0 \times 2^{**3} + 0 \times 2^{**2} + 1 \times 2^{**1} + 1 \times 2^{**0} = 51_{10}$$

33617 (base 8) is:

$$33617_8 = 3 \times 8^{**4} + 3 \times 8^{**3} + 6 \times 8^{**2} + 1 \times 8^{**1} + 7 \times 8^{**0} = 28439_{10}$$

ACF7 (base 16) is:

$$ACF7_{16} = 10 \times 16^{**3} + 12 \times 16^{**2} + 15 \times 16^{**1} + 7 \times 16^{**0} = 44279_{10}$$

2. Transforms decimal, octal, and hexadecimal to **binary**

Method: subtract largest power of 2 smaller than 81 until you reach 1:

$$81_{10} = 64 + 16 + 1 = 2^{**6} + 2^{**4} + 0 + 0 + 0 + 2^{**0} = 1010001_2$$

Tip: Best way to transform from decimal to octal is to go via Binary Octal representation to binary representation

$$745_8 = 7 \times 8^{**2} + 4 \times 8^{**1} + 5 \times 8^{**0}$$

In Binary: 111 100 101 111100101₂

$$D8F_{16} = 13 \times 16^{**2} + 8 \times 16^{**1} + 15 \times 16^{**0}$$

In Binary: 1101 1000 1111 110110001111₂

3. Transforms binary, decimal, and hexadecimal to **octal**

$$110100101010110_2 = 110\ 100\ 101\ 010\ 110_2 = 64526_8$$

$$161_{10} = 128 + 32 + 1 = 2^{**7} + 2^{**5} + 0 + 0 + 0 + 0 + 2^{**0} = 10100001_2 \rightarrow \textcolor{red}{0}10\ 100\ 001_2 \rightarrow 241_8$$

$$AEF78_{16} = 1010\ 1110\ 1111\ 0111\ 1000_2 = \textcolor{red}{0}10\ 101\ 110\ 111\ 101\ 111\ 000_2 = 2567570_8$$

4. Transforms binary, octal, and decimal to **hexadecimal**

$$101011111001110101011_2 = \textcolor{red}{000}1\ 0101\ 1111\ 0011\ 1010\ 1011_2 = 15F3AB_{16}$$

$$57672_8\ 101\ 111\ 110\ 111\ 010_2 \rightarrow \textcolor{red}{0}101\ 1111\ 1011\ 1010_2 \rightarrow 5FBA_{16}$$

$$6656_{10} = 4096 + 2048 + 512 =$$

$$2^{**12} + 2^{**11} + 0 + 2^{**9} + 0 + 0 + 0 + 0 + 0 + 0 + 0 + 0 = 1101000000000_2 \rightarrow \textcolor{red}{0000}1\ 1010\ 0000$$

$$0000 \rightarrow 1A00_{16}$$

Exercise:

1. Transform to binary

712_8

6634_8

236_{10}

729_{10}

9394_{16}

$AFED_{16}$

2. Transform to Decimal

1010110101001_2

1111111111111111_2

$CCDE_{16}$

800_{16}

7777_8

4000_8

3. Transform to octal

1010110101001_2

1111111111111111_2

$93F4_{16}$

$AFFF_{16}$

1111_{10}

9999_{10}

4. Transform to hexadecimal

$10101011101010001001010101_2$

1111111111111111_2

712_8

6634_8

1111_{10}

9999_{10}

5. Transform to base X to base X^k , $k = 1, 2, 3 \dots n$.

2212122221 (base 3) to its base 9 number

2212122221 (base 3) to its base 27 number

3123213231 (base 4) to its base 16 number

Solution:

1.

$$712_8 = 111001010_2$$

$$6634_8 = 110110011100_2$$

$$236_{10} = 11101100_2$$

$$729_{10} = 1011011001_2$$

$$9394_{16} = 1001001110010100_2$$

$$AFED_{16} = 101011111101101_2$$

2.

$$1010110101001_2 = 5545_{10}$$

$$1111111111111111_2 = 65535_{10}$$

$$CCDE_{16} = 52446_{10}$$

$$800_{16} = 2048_{10}$$

$$7777_8 = 4095_{10}$$

$$4000_8 = 2048_{10}$$

3.

$$1010110101001_2 = 12651_8$$

$$1111111111111111_2 = 177777_8$$

$$93F4_{16} = 111764_8$$

$$AFFF_{16} = 127777_8$$

$$1111_{10} = 2127_8$$

$$9999_{10} = 23417_8$$

4.

$$10101011101010001001010101_2 = 2AEA255_{16}$$

$$1111111111111111_2 = FFFF_{16}$$

$$712_8 = 1CA_{16}$$

$$6634_8 = D9C_{16}$$

$$1111_{10} = 457_{16}$$

$$9999_{10} = 270F_{16}$$

5.

$$2212122221 \text{ (base 3)} = 85587_9$$

$$2212122221 \text{ (base 3)} = 2NHP_{27}$$

$$3123213231 \text{ (base 4)} = DB9ED_{16}$$