



# Agenda & Readings

- ▶ **Agenda**
  - ▶ Using the Queue ADT to solve problems
  - ▶ A Circular Queue
  - ▶ The Deque Abstract Data Type
- ▶ **Reference:**
  - ▶ Textbook: Problem Solving with Algorithms and Data Structures
    - Chapter 3: Basic Data Structures



## COMPSCI 105 S1 2017 Principles of Computer Science

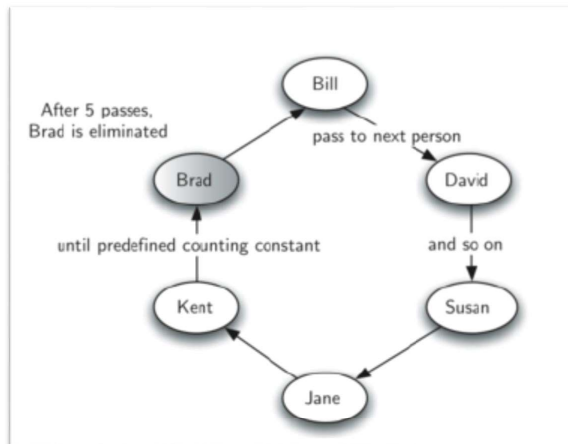
16 Queue(2)



### 16.1 Applications

## Simulation: Hot Potato

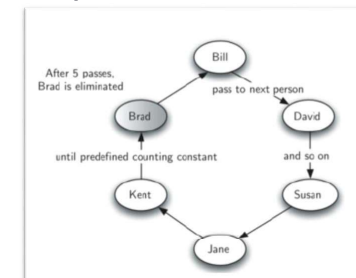
- ▶ **Example (six persons game):**



### 16.1 Applications

## Simulation: Hot Potato

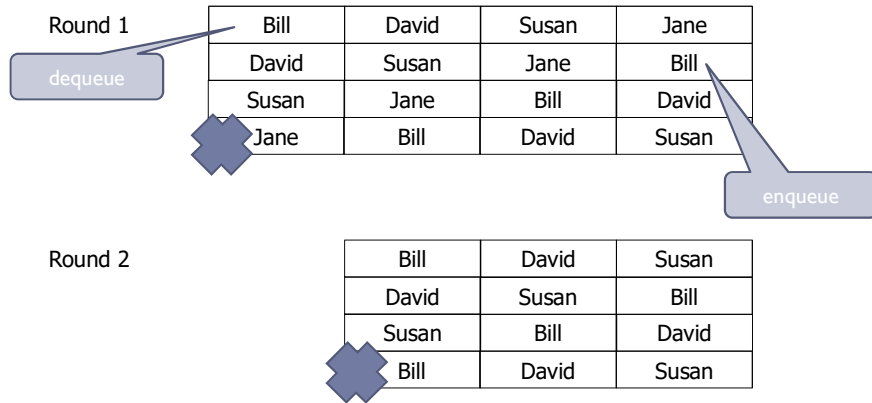
- ▶ **Example (six persons game):**
  - ▶ Children form a circle and pass an item from neighbour to neighbour as fast as they can
  - ▶ At a certain point in the game, the action is stopped and the child who has the item (the potato) is removed from the circle
  - ▶ Play continues until only one child is left





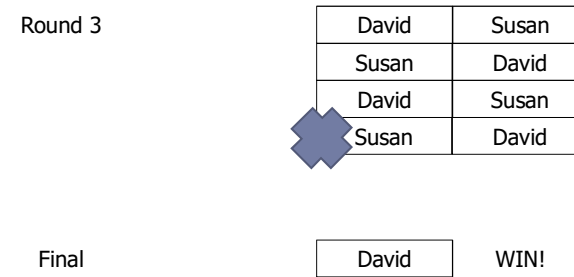
# Simulation: Hot Potato

▶ Example (hotPotato(['Bill, David, Susan, Jane], 3)):



# Simulation: Hot Potato

▶ Example (hotPotato(['Bill, David, Susan, Jane], 3)):



# Simulation: Hot Potato

▶ Code:

```
def hotPotato(namelist, num):
    simqueue = Queue()
    for name in namelist:
        simqueue.enqueue(name)
    while simqueue.size() > 1:
        for i in range(num):
            simqueue.enqueue(simqueue.dequeue())
        simqueue.dequeue()
    return simqueue.dequeue()
```

Move element from the front of the queue to the end

Return the name when there is only ONE name remains in the queue



# Circular Queue

▶ What is the Big-O performance of enqueue and dequeue of the implementation using Python List?

▶ enqueue(...):  $O(n)$

We have to shift all list elements by one position to make room for the new item

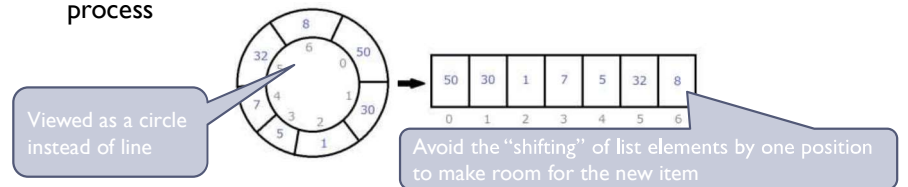
▶ Shifting array elements to the right after each addition – too Expensive!

▶ dequeue():  $O(1)$

▶ Another Implementation: **Circular Queue**

▶ enqueue & dequeue :  $O(1)$

▶ Items can be added/removed without shifting the other items in the process

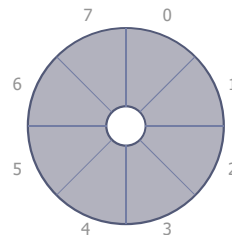


- ▶ Uses a Python list data structure to store the items in the queue
- ▶ There are three critical variables:
  - ▶ **front**: indicates the location of the item at the front
  - ▶ **back**: indicates the location of the item at the back
  - ▶ **count**: indicates the number of items in the queue
- ▶ The list has an initial capacity (all elements None)

- ▶ Keeps an index of the current **front** of the queue and of the current **back** of the queue
  - ▶ set **front** to 0 To initialize the queue
  - ▶ set **back** to  $\text{MAX\_QUEUE} - 1$
  - ▶ set **count** to 0
- ▶ New items are **enqueued** at the **back** index position
- ▶ Items are **dequeued** at the **front** index position.
- ▶ A **counting** of the queue items to detect queue-full and queue-empty conditions

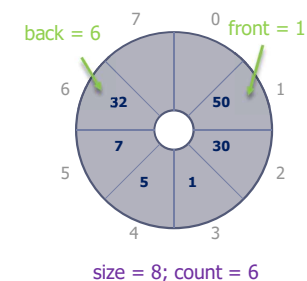
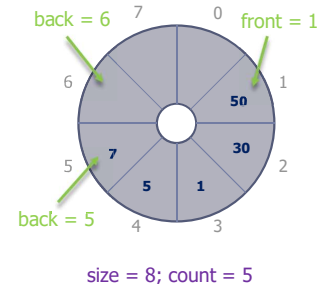
- ▶ Queue-empty:
  - ▶ **front** is one slot ahead of **back**
- ▶ When either front or back advances past  $\text{MAX\_QUEUE} - 1$ , it wraps around to 0
- ▶ The wrap-around effect: by using Modulus (%) arithmetic operator

```
def enqueue(self, item): # if not full
    self.back = (self.back + 1) % self.MAX_QUEUE
    self.items[self.back] = item
    self.count += 1
def dequeue(self): # if not empty
    item = self.items[self.front]
    self.front = (self.front + 1) % self.MAX_QUEUE
    self.count -= 1
    return item
```



- ▶ Example:
  - ▶ `q.enqueue(32)`
    - ▶ **back** is advanced by one position
    - ▶ New item is inserted at the position of **back**
    - ▶ **count** is incremented by 1

```
def enqueue(self, item): # if not full
    self.back = (self.back + 1) % self.MAX_QUEUE
    self.items[self.back] = item
    self.count += 1
```

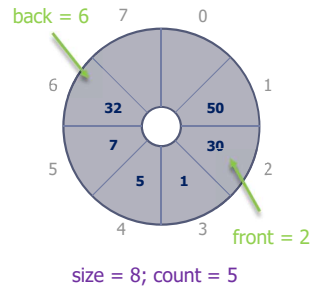
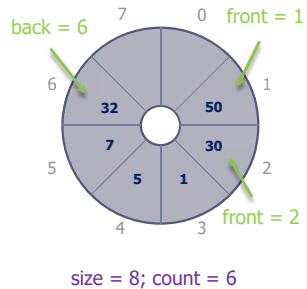


16.2 Circular Queue  
Dequeue

▶ Example:

- ▶ q.dequeue()
  - ▶ Value in front position is returned
  - ▶ front is advanced by 1
  - ▶ count is decremented by 1

```
def dequeue(self): # if not empty
    item = self.items[self.front]
    self.front = (self.front + 1) % self.MAX_QUEUE
    self.count -= 1
    return item
```



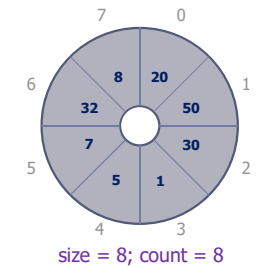
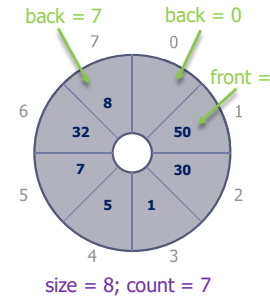
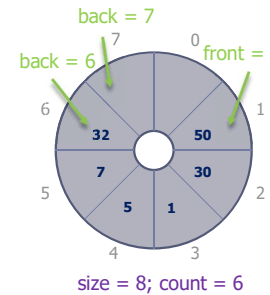
16.2 Circular Queue  
Enqueue

▶ q.enqueue(8)

- ▶ After running the first enqueue, back = 7

▶ q.enqueue(20)

- ▶ After running the second enqueue, back = 0 as the "back" is wrapped around the list



16.2 Circular Queue  
Full & Empty

- ▶ front and back cannot be used to distinguish between queue-full and queue-empty conditions for a circular array

q = QueueCircular(8)

q.enqueue(5)  
q.enqueue(2)  
q.enqueue(1)  
q.enqueue(7)  
q.enqueue(9)

q.dequeue()  
q.dequeue()  
q.dequeue()  
q.dequeue()

back = front - 1

16.2 Circular Queue  
Full & Empty

- ▶ front and back cannot be used to distinguish between queue-full and queue-empty conditions for a circular array

```
q = QueueCircular(8)
q.enqueue(5)
q.enqueue(2)
q.enqueue(1)
q.enqueue(7)
q.enqueue(9)
q.enqueue(1)
q.enqueue(7)
q.enqueue(9)
```

```
def is_empty():
    return self.count == 0
```

```
def is_full():
    return self.MAX_QUEUE <= self.count
```

- ▶ What are the values of “front” and “back” after executing the following code fragment?

```

q = Queuercircular(10)
q.enqueue(12)
q.enqueue(17)
q.enqueue(25)
q.enqueue(11)
q.dequeue()
q.dequeue()
q.enqueue(30)
    
```

- ▶ Deque - Double Ended Queue
  - ▶ A deque is an ordered collection of items where items are added and removed from either end, either front or back
  - ▶ The newest item is at one of the ends

- ▶ What are the operations which can be used with a Deque Abstract Data?
- ▶ Create an empty deque:
- ▶ Determine whether a deque is empty:
- ▶ Add a new item to the deque:
  - ▶ `add_front()`
  - ▶ `add_rear()`
- ▶ Remove from the deque the item that was added earliest:
  - ▶ `remove_front()`
  - ▶ `remove_rear()`

- ▶ We use a python **List** data structure to implement the deque

```

class Deque:
    def __init__(self):
        self.items = []
    ...
    def add_front(self, item):
        self.items.append(item)
    def add_rear(self, item):
        self.items.insert(0,item)
    def remove_front(self):
        return self.items.pop()
    def remove_rear(self):
        return self.items.pop(0)
    
```

**Big-O?**  
`add_front()/remove_front(): O(1)`  
`add_rear()/remove_rear(): O(n)`



## Code Example

## ▶ Code:

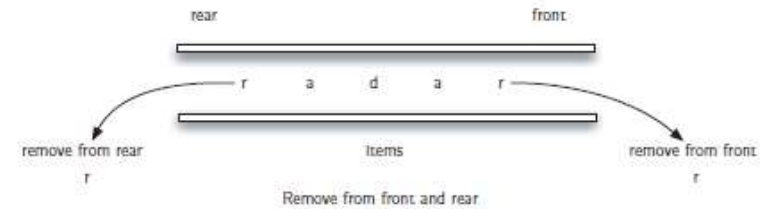
<pre> d.is_empty() d.add_rear(4) d.add_rear('dog') d.add_front('cat') d.add_front(True) d.size() d.is_empty() d.add_rear(8.4) d.remove_rear() d.remove_front() </pre>	<pre> d = [] d = [4] d = ['dog', 4] d = ['dog', 4, 'cat'] d = ['dog', 4, 'cat', True] d = ['dog', 4, 'cat', True] d = ['dog', 4, 'cat', True] d = ['dog', 4, 'cat', True] d = [8.4, 'dog', 4, 'cat', True] d = ['dog', 4, 'cat', True] d = ['dog', 4, 'cat'] </pre>	<pre> True 4 False 8.4 True </pre>
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## Application: Palindrome Checker

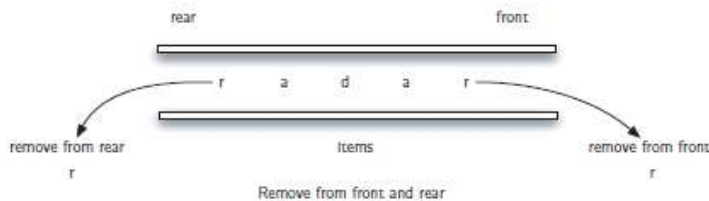
▶ A string which reads the same either left to right, or right to left is known as a palindrome

- ▶ Radar
- ▶ deed
- ▶ A dog, a plan, a canal: pagoda



## Palindrome Checker - Algorithm

- ▶ Create a **deque** to store the characters of the string
  - ▶ The **front** of the **deque** will hold the **first** character of the string and the **rear** of the **deque** will hold the **last** character
- ▶ Remove both of them directly, we can compare them and continue only if they match
  - ▶ If we can keep matching first and the last items, we will eventually either **run out of characters** or be left with a **deque of size 1**
    - ▶ In either case, the string must be a palindrome



## Palindrome Checker - Examples

- ▶ `print(pal_checker("lsdkjfskf"))`
  - ▶ Queue: f, k, s, f, j, k, d, s, l
  - ▶ 1<sup>st</sup> round: compare **f** and **l** => **FALSE**, STOP
- ▶ `print(pal_checker("radar"))`
  - ▶ Queue: r, a, d, a, r
  - ▶ 1<sup>st</sup> round: compare **r** (front) and **r** (back)
  - ▶ 2<sup>nd</sup> round: compare **a** (front) and **a** (back)
  - ▶ 3<sup>rd</sup> round: `size() = 1`, STOP, return **TRUE**



## Palindrome Checker - Codes

### ▶ Check:

- ▶ The front of the deque (the first character of the string)
- ▶ The rear of the deque (the last character of the string)

```
still_equal = True
while char_deque.size() > 1 and still_equal:
    first = char_deque.remove_front()
    last = char_deque.remove_rear()
    if first != last:
        still_equal = False
return still_equal
```



## Summary

- ▶ To distinguish between the queue-full and queue-empty conditions in a queue implementation that uses a circular array
  - ▶ By counting the number of items in the queue
- ▶ Models of real-world systems often use queues