

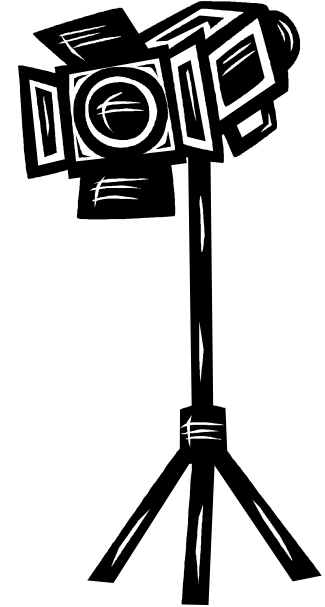
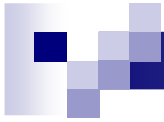
# Computer Graphics: Illumination I

Part 2 – Lecture 4



# Today's Outline

- Illumination and Shading
- The Phong Illumination Model
  - Ambient Reflection
  - Diffuse Reflection
  - Specular Reflection



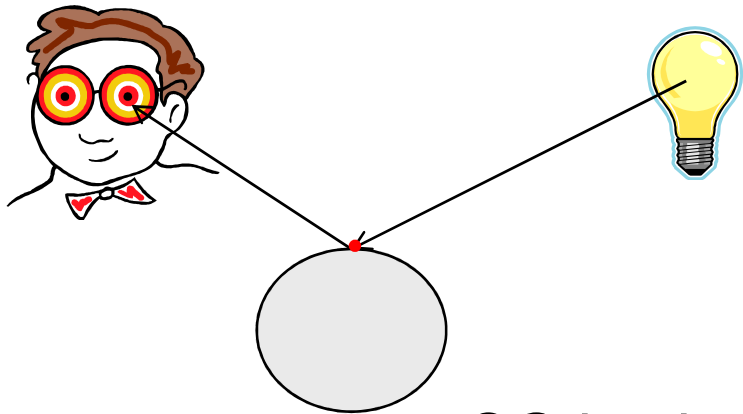
# ILLUMINATION AND SHADING

# Illumination vs. Shading

NB: Hill  
doesn't make  
this distinction

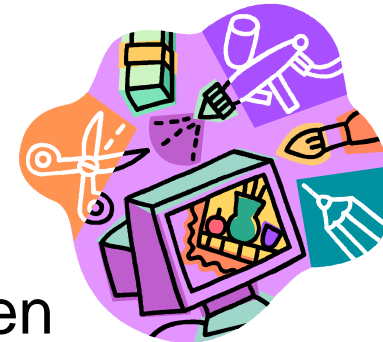
## Illumination Model

- What color is the surface?  
→ surface reflection model
- Use equations from physics  
(realistic but time consuming)
- Or use good approximations  
(much faster to compute!)



## Shading Model

- How do we calculate the color at each pixel?  
→ pixel shading algorithm
- Using exact illumination model for every pixel usually too slow (and often unnecessary)
- Apply the illumination model only sometimes and interpolate



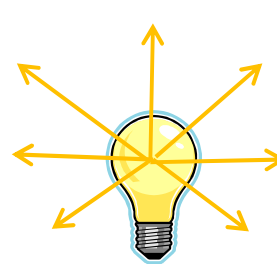
CG is about a trade-off between  
**visual realism vs. computing time**

# Introduction to Illumination Models

- Where does the light come from? → Light sources

- **Point sources**

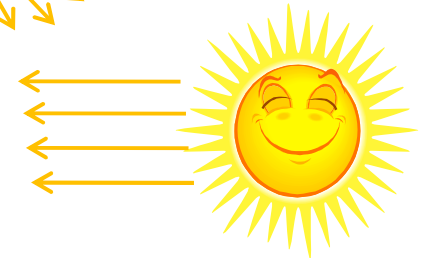
- e.g. lamp, headlight, spotlight



- **Directional sources**

- (like a far away point source, rays are parallel)

- e.g. sun



- What happens to the light?

- **Reflection:** ray bounces off a surface

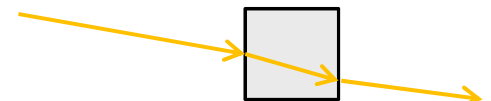
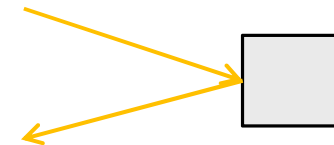
- (most important for CG)

- **Absorption:** ray energy taken up by an object,

- e.g. as heat (not important for CG)

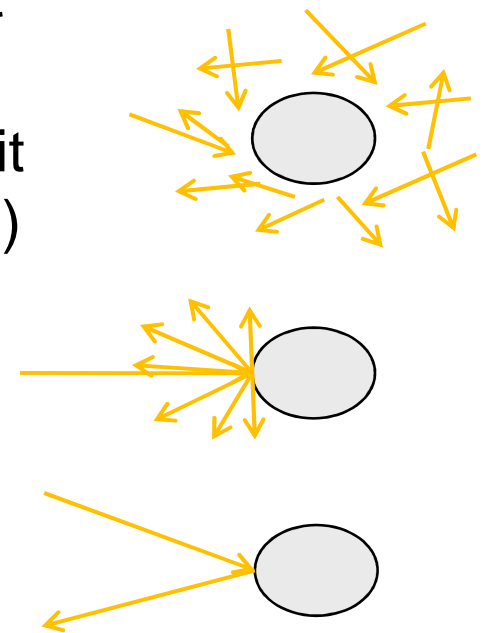
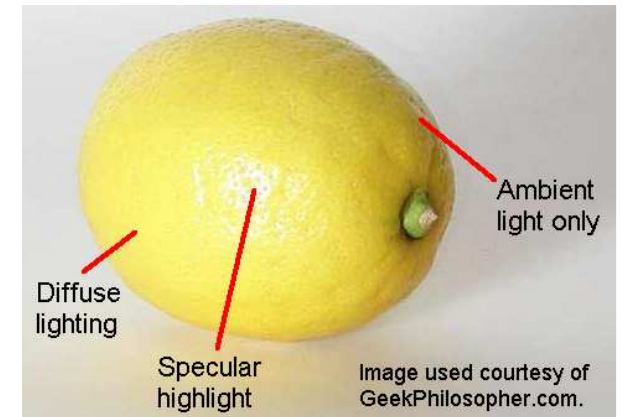
- **Transmission:** ray passes through an object,

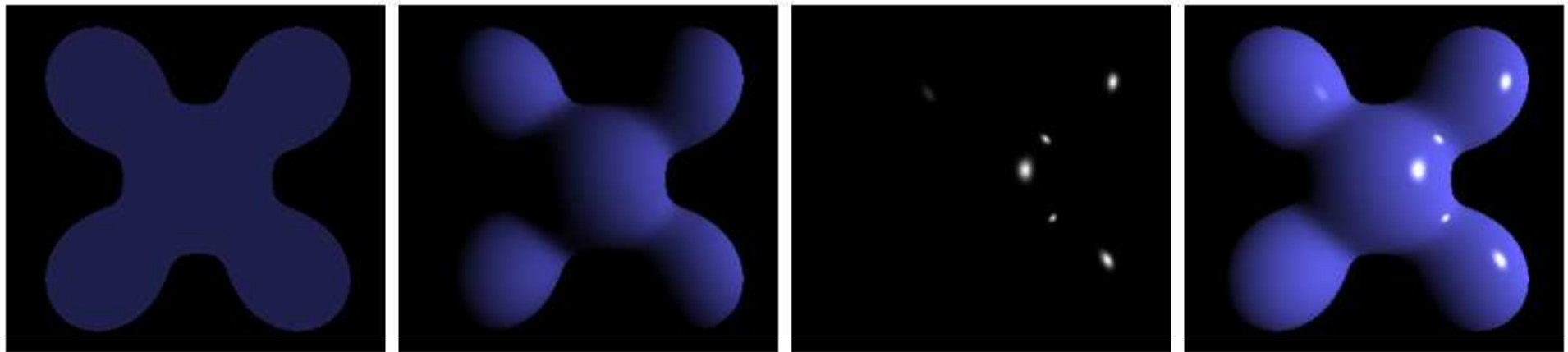
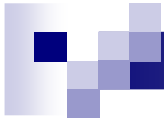
- e.g. water, glass (often not considered in CG)



# Types of Light Reflection

- In the real world:
  - Light reflected unlimited number of times
  - Reflections change the appearance of the light
- In CG we need to keep computation time short:
  - Can often calculate only one reflection per vertex
  - Consider different light appearances as different types of reflection
- **Ambient reflection:** light reflected so many times, it is everywhere (like uniform background illumination)
- **Diffuse reflection:** light scattered from one point equally (more or less) into all directions
- **Specular reflection:** light rays bounce off in pretty much only one direction (like from a mirror)
- Type of reflection can depend on light source characteristics and the material of the object



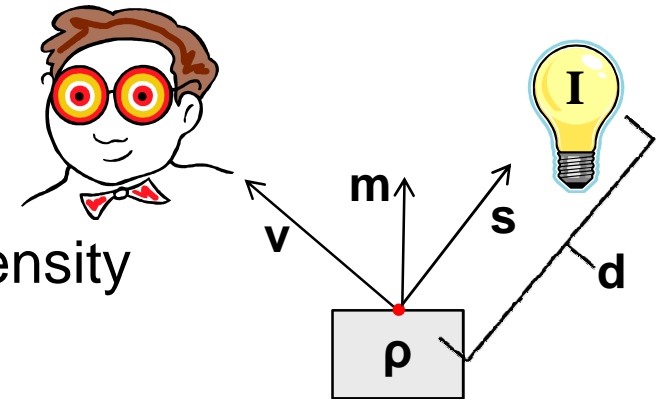


Ambient + Diffuse + Specular = Phong Reflection

# PHONG ILLUMINATION MODEL

# Phong Illumination Model

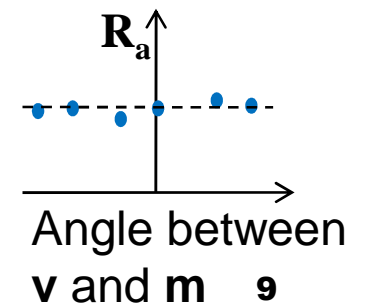
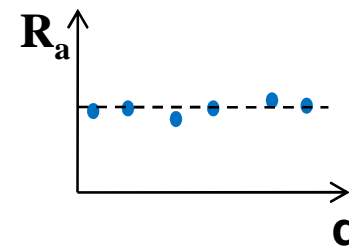
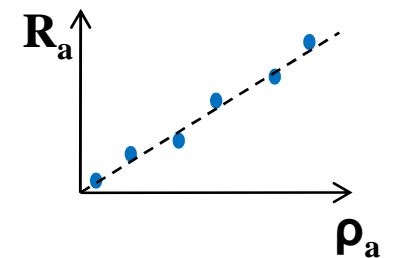
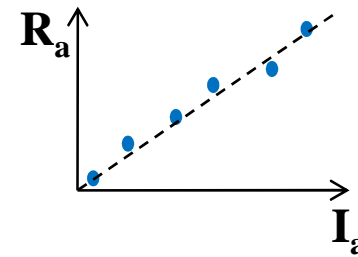
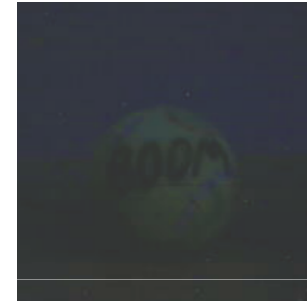
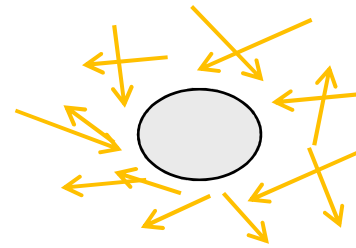
- Invented by Bui Tuong-Phong, PhD at Univ. of Utah 1973
- Idea: calculate intensity  $I$  (and color) of visible light at a point as the sum of ambient, diffuse and specular reflection
- Variables taken into account:
  - Intensities (and colors) for incident light:  
 $I_a$ ,  $I_d$ ,  $I_s$  for ambient, diffuse and specular intensity
  - Surface normal vector  $\mathbf{m}$
  - Vector  $\mathbf{s}$  describing the direction to the light source
  - Distance  $d$  to light source
  - Vector  $\mathbf{v}$  describing the direction to the viewer
  - Reflection coefficients of the surface material  
 $\rho_a$ ,  $\rho_d$ ,  $\rho_s$  for ambient, diffuse and specular reflection  
(actually separate coefficients for RGB colors)





# Ambient Reflection

- **Source:** no single point or directional source  
All the scattered “background” light,  
e.g. sunlight, lamps, moonlight, star light, ...
- **Direction of reflection:** all directions  
(it is scattered everywhere)
- **Experiment:** turn out room lights
  - No direct light sources
  - Just some indirect light,  
e.g. from gap under a door
  - Keeping all other variables constant,  
we change intensity, view direction,  
material, etc. and see what happens  
to the reflected ambient light  $R_a$



# Ambient Reflection

We construct an equation for  $\mathbf{R}_a$ :

$$\mathbf{R}_a = \mathbf{I}_a \rho_a$$

How to deal with colors (RGB)?

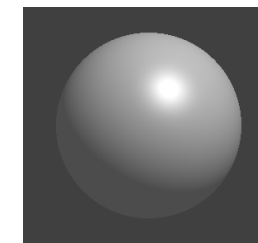
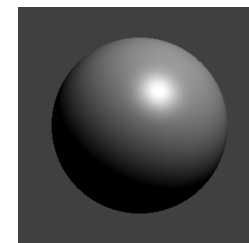
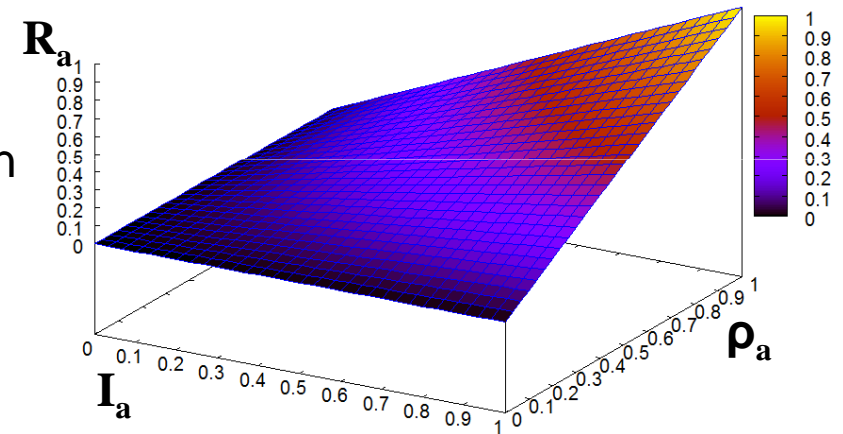
- Instead of just  $\mathbf{I}_a$ , use  $\mathbf{I}_{ar}$ ,  $\mathbf{I}_{ag}$ ,  $\mathbf{I}_{ab}$   
→ colored light
- Instead of just  $\rho_a$ , use  $\rho_{ar}$ ,  $\rho_{ag}$ ,  $\rho_{ab}$   
→ colored materials
- Compute reflected light for each color:

$$\mathbf{R}_{ar} = \mathbf{I}_{ar} \rho_{ar}$$

$$\mathbf{R}_{ag} = \mathbf{I}_{ag} \rho_{ag}$$

$$\mathbf{R}_{ab} = \mathbf{I}_{ab} \rho_{ab}$$

Variable	Influence on $\mathbf{R}_a$
$\mathbf{I}_a$	Proportional
$\rho_a$	Proportional
$\mathbf{d}$	No influence
$\mathbf{v}$	No influence

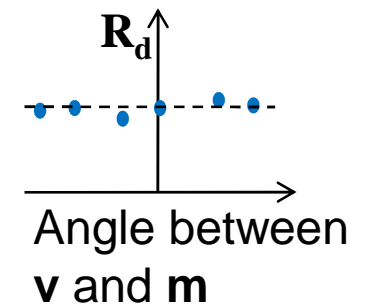
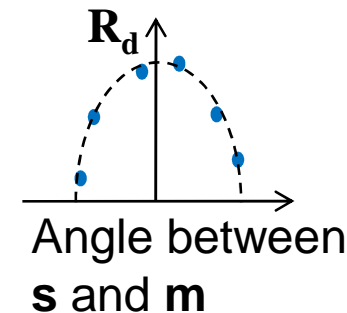
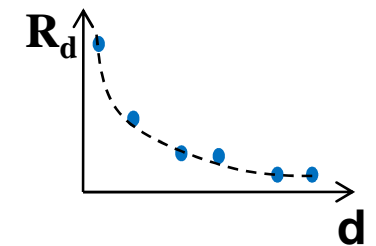
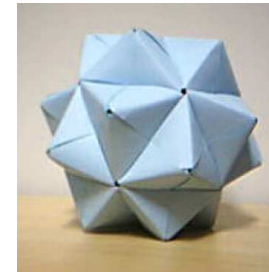
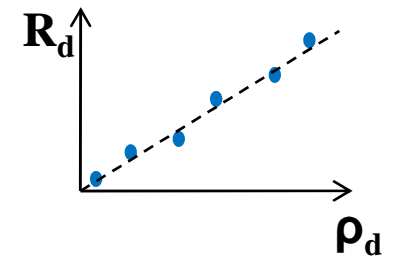
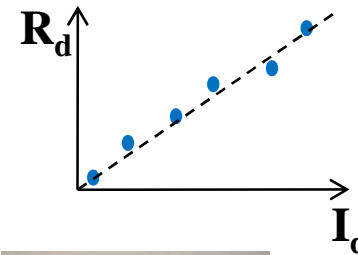
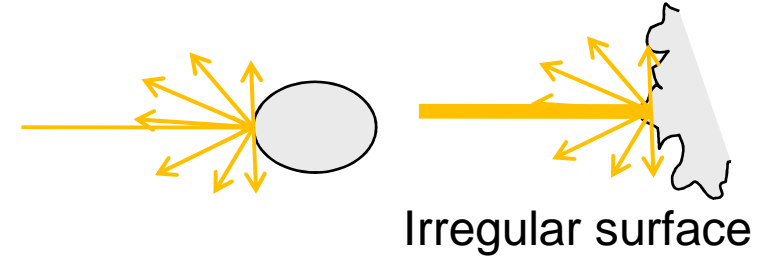


No ambient light      A lot of ambient light

# Diffuse Reflection

- **Source:** one or more point or directional sources
- **Direction of reflection:** all directions (it is scattered everywhere)
- **Experiment:** turn out room lights
  - Use only “soft” light sources where light is already scattered a little (but not everywhere), e.g. light bulb
  - Shine on rough surface, e.g. rough wood, stone or cloth
  - Keeping all other variables constant, we change intensity, view direction, material, etc. and see what happens to the reflected ambient light  $\mathbf{R}_a$

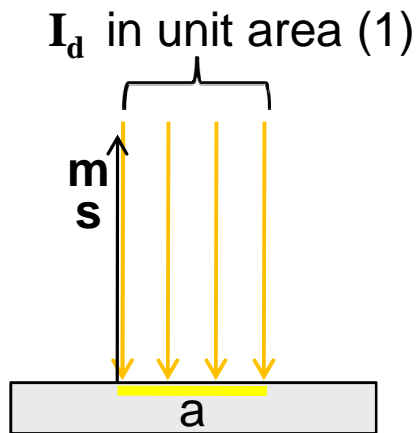
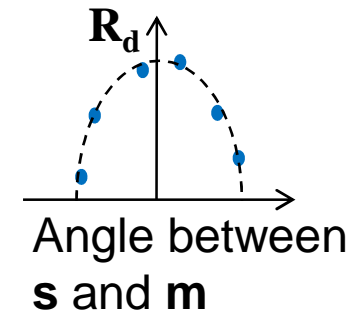
Under microscope:



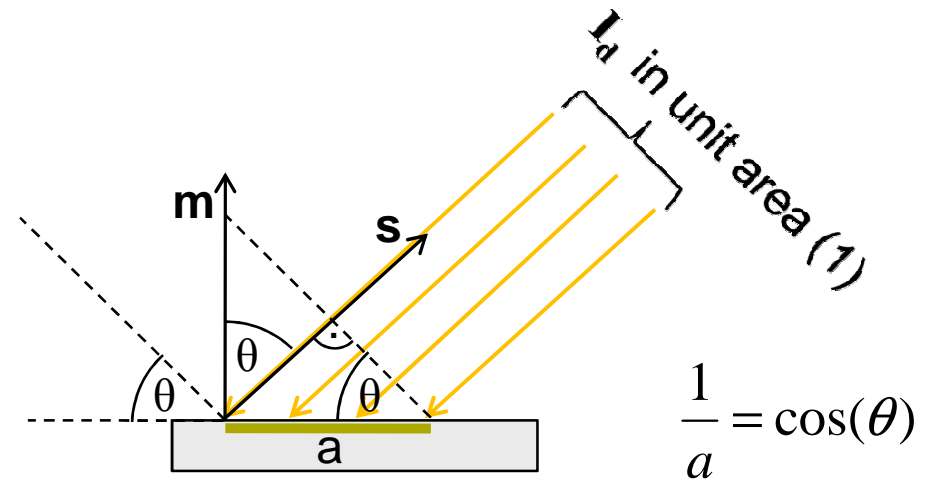
# Lambert's Law

Why does  $R_d$  depend on the angle between  $s$  and  $m$ ?

- $R_d$  proportional to incoming  $I_d$  **per unit area**
- Rays spread over larger area means less reflection per unit area



At angle 0 between  $s$  and  $m$ , rays hit area of the same size, i.e.  $a=1$  and  $R_d \sim I_d$



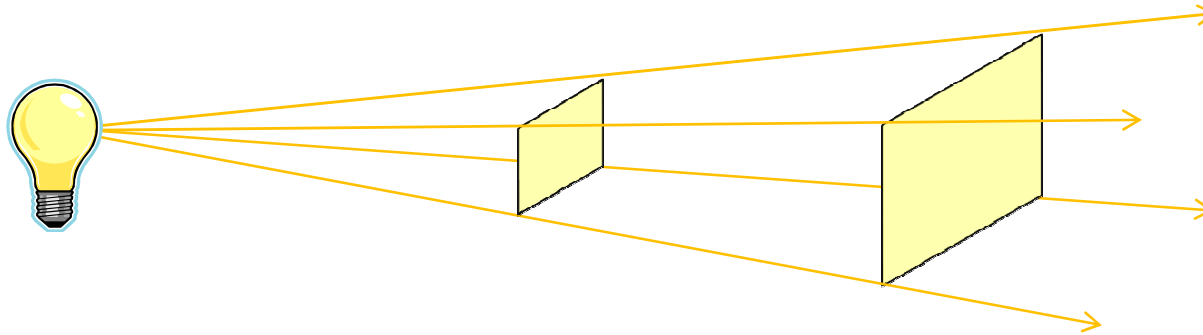
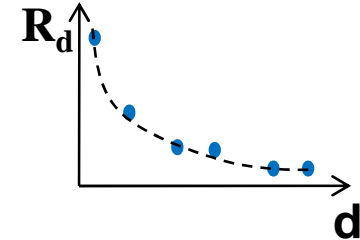
At angle  $\theta$  between  $s$  and  $m$ , rays hit area  $a$  of the size  $1/\cos(\theta)$

$$R_d \sim \frac{I_d}{1/\cos(\theta)} = I_d \cos(\theta) = I_d \frac{s \cdot m}{|s||m|}$$

# Distance from Light Source

In the real world:

- Intensity of light from a point source decreases quadratically with  $d$ , i.e. divide intensity by  $d^2$
- Area through which the rays pass grows quadratically with  $d$



In CG:

- Dividing intensity by  $d^2$  would make intensities too small
- CG “hack” is to divide by  $(k_c + k_l d + k_q d^2)$
- $k_c$ ,  $k_l$ ,  $k_q$  are programmer-chosen constants (no real world meaning)
- Typically,  $k_c = 1.0$ ,  $0 < k_l < 1$  and  $k_q = 0$ , but usually they have to be tuned so that it looks good

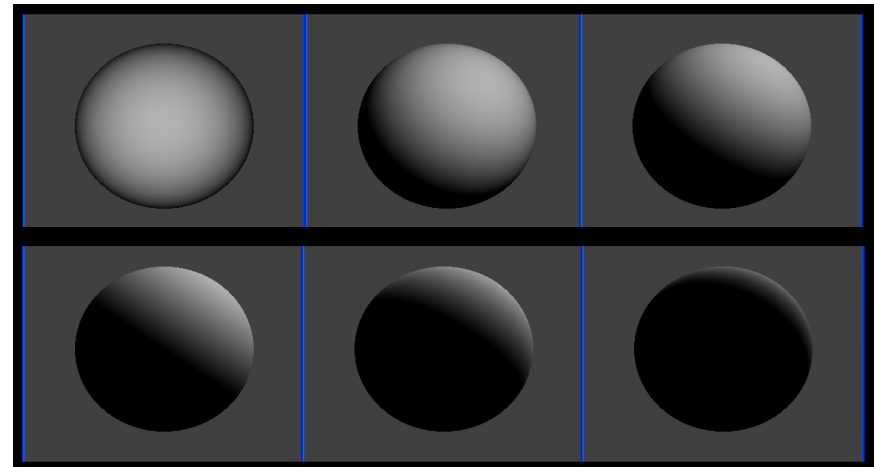
# Diffuse Reflection

We construct an equation for  $\mathbf{R}_d$ :

$$\mathbf{R}_d = \mathbf{I}_d \rho_d \frac{s \cdot m}{|s||m|} / (k_c + k_l d + k_q d^2)$$

- Add color by calculating  $\mathbf{R}_{dr}$ ,  $\mathbf{R}_{dg}$ ,  $\mathbf{R}_{db}$  using  $\mathbf{I}_{dr}$ ,  $\mathbf{I}_{dg}$ ,  $\mathbf{I}_{db}$  and  $\rho_{dr}$ ,  $\rho_{dg}$ ,  $\rho_{db}$  instead of just  $\mathbf{R}_d$ ,  $\mathbf{I}_d$  and  $\rho_d$

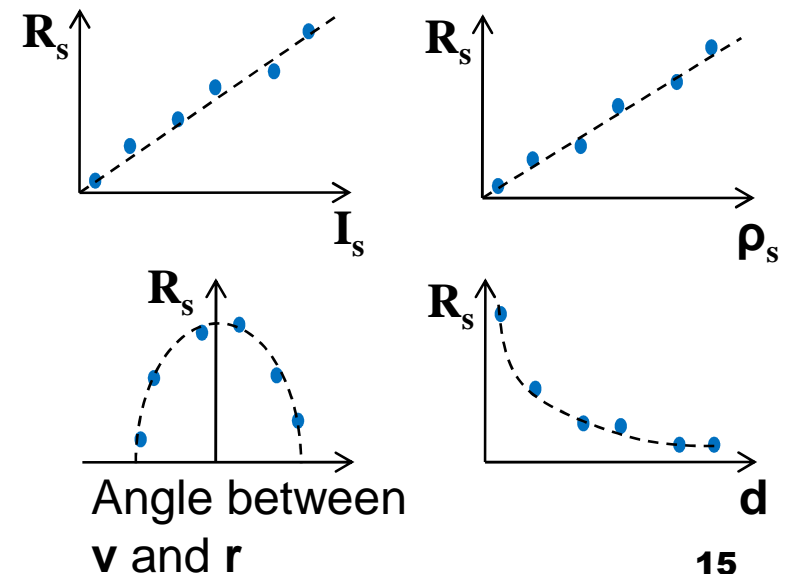
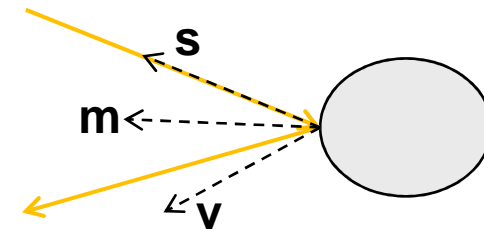
Variable	Influence on $\mathbf{R}_d$
$\mathbf{I}_a$	Proportional
$\rho_d$	Proportional
$\mathbf{s}$	Lambert's law
$d$	Divide by ( $k_c + k_l d + k_q d^2$ )
$\mathbf{v}$	No influence



Lambertian spheres  
(diffuse reflectors)

# Specular Reflection

- **Source:** one or more point or directional sources
- **Direction of reflection  $r$ :** mostly only one (very little scattering) →  $r$  is calculated from  $s$  and  $m$
- **Experiment:** turn out room lights
  - Use only hard light sources where light is not scattered, e.g. a spotlight
  - Shine on glossy surface, e.g. polished metal
  - Keeping all other variables constant, we change intensity, view direction, material, etc. and see what happens to the reflected ambient light  $R_a$



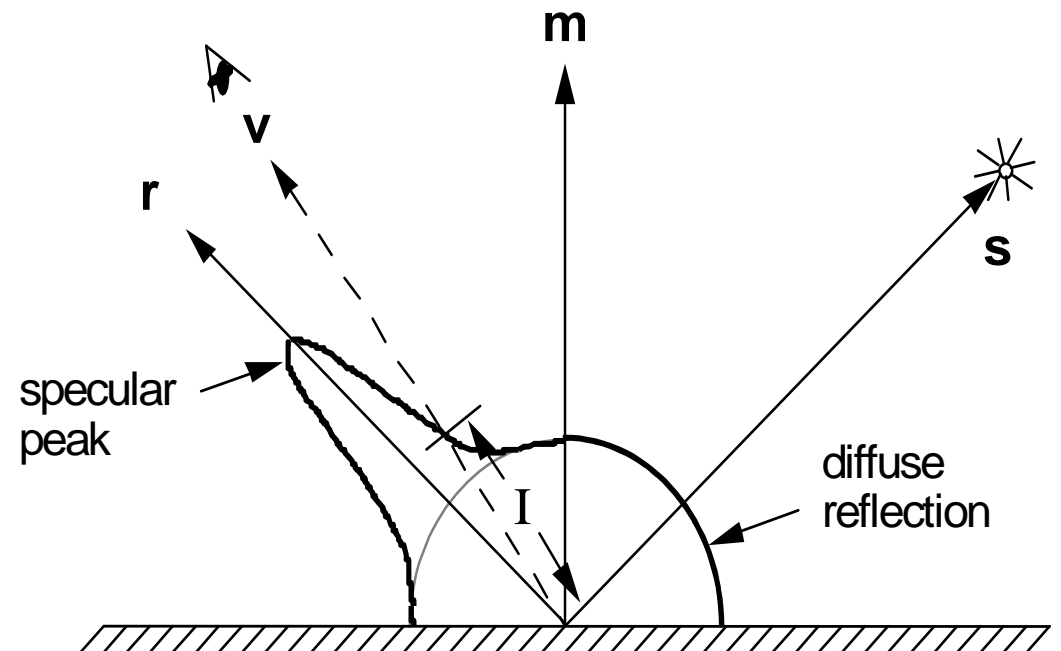
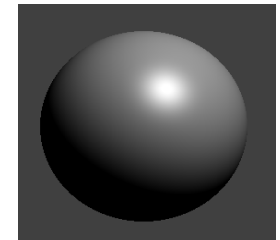
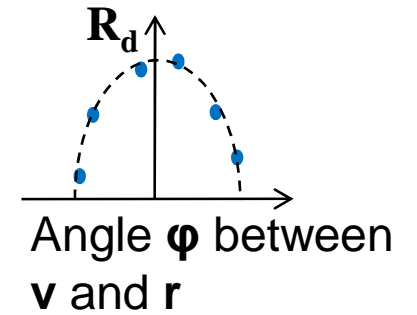
# Specular Highlight

Angle  $\varphi$  between  $\mathbf{v}$  and  $\mathbf{r}$ :

- Looking directly into the reflected ray ( $0^\circ$ ) = very bright
- The farther the reflected ray away from the eye, the darker
- Result: a bright spot where the light is reflected directly into the eye ( $\rightarrow$  highlight)
- Model as cosine function:

$$\mathbf{R}_d \text{ grows with } \cos(\varphi) = \frac{\mathbf{v} \cdot \mathbf{r}}{|\mathbf{v}| |\mathbf{r}|}$$

- But  $\mathbf{R}_d$  is always positive, so if  $\cos(\varphi)$  negative set  $\mathbf{R}_d$  to 0

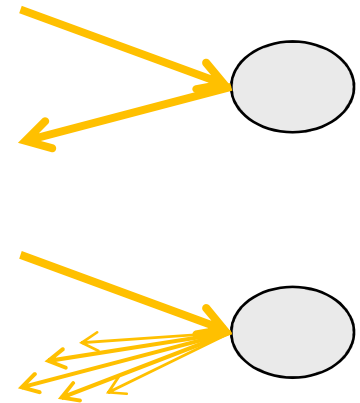




# Shininess $\alpha$

Different behaviors of specular surfaces:

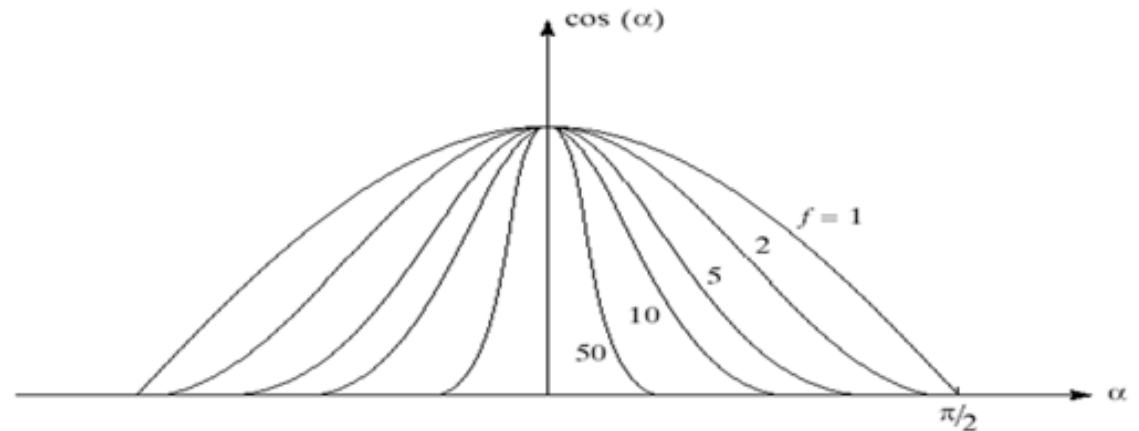
- Some glossy materials reflect perfectly (e.g. a mirror), i.e. one ray is pretty much reflected as one ray  
→ small highlight (bigger shininess  $\alpha$ )
- Other materials scatter incoming rays a little bit, i.e. several outgoing rays close together  
→ bigger highlight (smaller shininess  $\alpha$ )



Shininess  $\alpha$  of object surface:

- “Focus” of specular reflection
- Use as exponent of our cosine specular reflection formula:

$$\cos(\varphi)^\alpha = \left( \frac{v \cdot r}{|v||r|} \right)^\alpha$$



# Specular Reflection

We construct an equation for  $\mathbf{R}_d$ :  
(assuming we have calculated  $\mathbf{r}$  from  $\mathbf{s}$  and  $\mathbf{m}$ )

$$\mathbf{R}_s = \mathbf{I}_s \rho_s \left( \frac{\mathbf{v} \cdot \mathbf{r}}{|\mathbf{v}| |\mathbf{r}|} \right)^\alpha / (k_c + k_l d + k_q d^2)$$

Variable	Influence on $\mathbf{R}_s$
$\mathbf{I}_s$	Proportional
$\rho_s$	Proportional
$\mathbf{r}$ and $\mathbf{v}$	Highlight intensity
$\alpha$	Highlight size
$d$	Divide by ( $k_c + k_l d + k_q d^2$ )

- Add color by calculating  $\mathbf{R}_{sr}$ ,  $\mathbf{R}_{sg}$ ,  $\mathbf{R}_{sb}$   
using  $\mathbf{I}_{sr}$ ,  $\mathbf{I}_{sg}$ ,  $\mathbf{I}_{sb}$  and  $\rho_{sr}$ ,  $\rho_{sg}$ ,  $\rho_{sb}$   
instead of just  $\mathbf{R}_s$ ,  $\mathbf{I}_s$  and  $\rho_s$

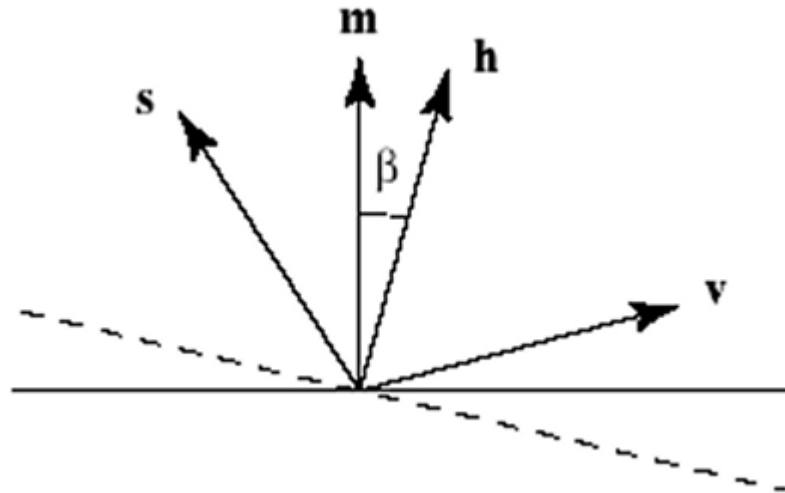


# Specular Reflection Optimized

Instead of calculating  $\mathbf{r}$ , use simpler **halfway-vector**  $\mathbf{h}$  for highlight:

$$\left( \frac{\mathbf{h} \cdot \mathbf{m}}{|\mathbf{h}| |\mathbf{m}|} \right)^\alpha \quad \text{with } \mathbf{h} = \text{normalized } (\mathbf{s} + \mathbf{v}) \\ (\rightarrow \mathbf{h} \text{ is half way between } \mathbf{s} \text{ and } \mathbf{v})$$

- Consider angle between  $\mathbf{h}$  and  $\mathbf{m}$  instead of angle between  $\mathbf{r}$  and  $\mathbf{v}$ 
  - If  $\mathbf{h}$  is exactly on  $\mathbf{m}$  ( $0^\circ$ ) then reflection directly into the eye ( $\mathbf{r}$  on  $\mathbf{v}$ )
  - Greater angle between  $\mathbf{h}$  and  $\mathbf{m}$   $\rightarrow$  greater angle between  $\mathbf{r}$  and  $\mathbf{v}$
- Not mathematically identical, but same general properties
- Larger highlight for any given  $\alpha$  because angle grows slower
- Used by OpenGL



# Final Phong Equation

- Achromatic version:

$$\mathbf{R} = \mathbf{I}_a \rho_a + \left( \mathbf{I}_d \rho_d \frac{s \cdot m}{|s||m|} + \mathbf{I}_s \rho_s \left( \frac{h \cdot m}{|h||m|} \right)^\alpha \right) / (k_c + k_l d + k_q d^2)$$

- Chromatic version (RGB):

$$\mathbf{R}_r = \mathbf{I}_{ar} \rho_{ar} + \left( \mathbf{I}_{dr} \rho_{dr} \frac{s \cdot m}{|s||m|} + \mathbf{I}_{sr} \rho_{sr} \left( \frac{h \cdot m}{|h||m|} \right)^\alpha \right) / (k_c + k_l d + k_q d^2)$$

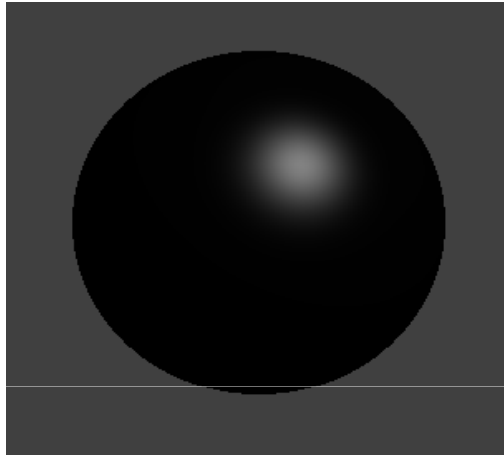
$$\mathbf{R}_g = \mathbf{I}_{ag} \rho_{ag} + \left( \mathbf{I}_{dg} \rho_{dg} \frac{s \cdot m}{|s||m|} + \mathbf{I}_{sg} \rho_{sg} \left( \frac{h \cdot m}{|h||m|} \right)^\alpha \right) / (k_c + k_l d + k_q d^2)$$

$$\mathbf{R}_b = \mathbf{I}_{ab} \rho_{ab} + \left( \mathbf{I}_{db} \rho_{db} \frac{s \cdot m}{|s||m|} + \mathbf{I}_{sb} \rho_{sb} \left( \frac{h \cdot m}{|h||m|} \right)^\alpha \right) / (k_c + k_l d + k_q d^2)$$

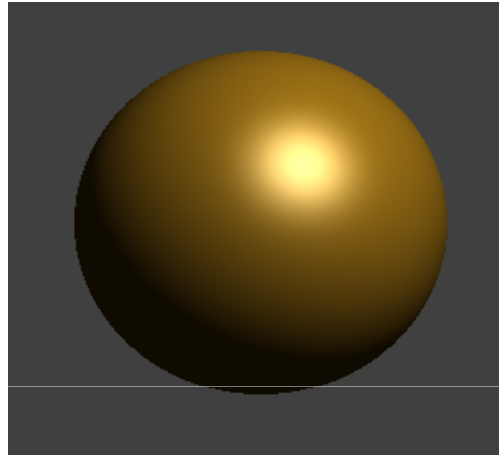
- For multiple light sources: add up the reflected light

# Phong Shading Examples

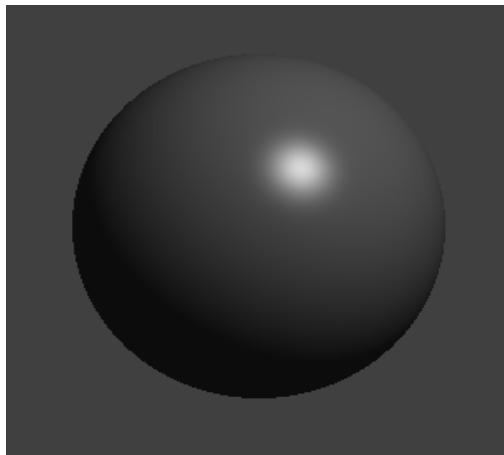
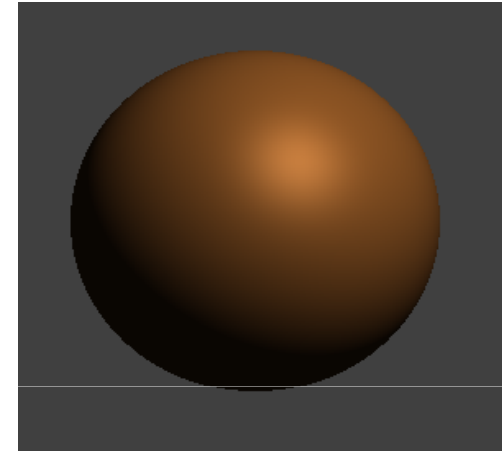
Black Plastic



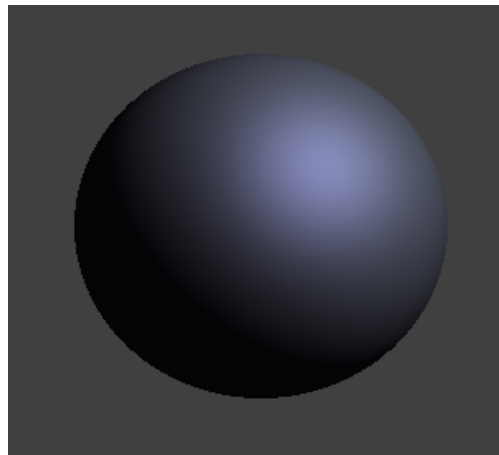
Brass



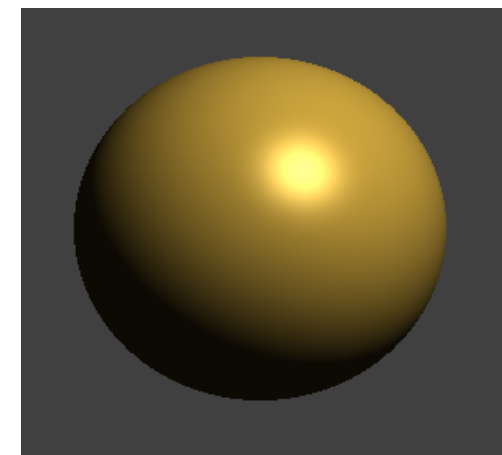
Bronze



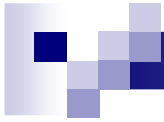
Chrome



Pewter



Gold



# SUMMARY



# Summary

- **Illumination models:** what color does a surface have?
- **Shading models:** how to calculate the color of each pixel?
- **Phong illumination model:**  
calculate intensity  $I$  (and color) of visible light at a point as the sum of ambient, diffuse and specular reflection
  - Ambient reflection: light scattered everywhere (background illumination)
  - Diffuse reflection: light reflected into all directions on rough surface
  - Specular reflection: light reflected directly into the eye

## References:

- Phong Illumination Model: Hill, Chapter 8.2, pp. 381-391



# Quiz

1. Why does the view direction not matter for diffusely reflected light?
2. What does Lambert's law say? Where do we use it?
3. What does the shininess parameter  $\alpha$  do?