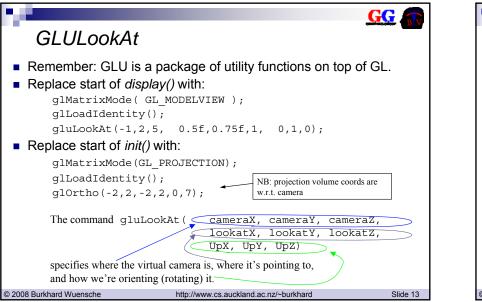
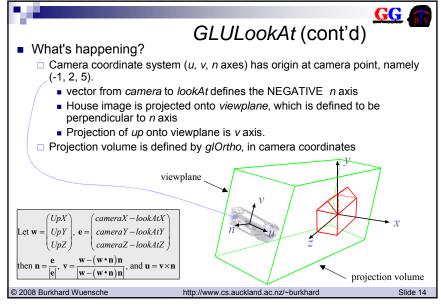
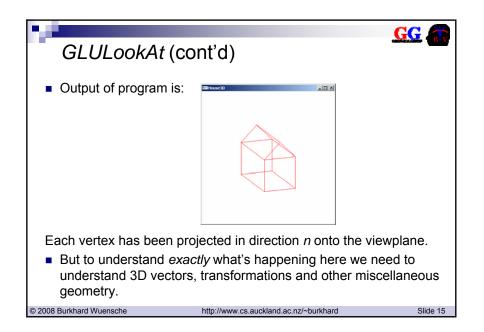


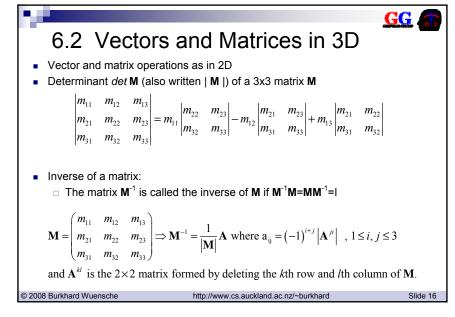
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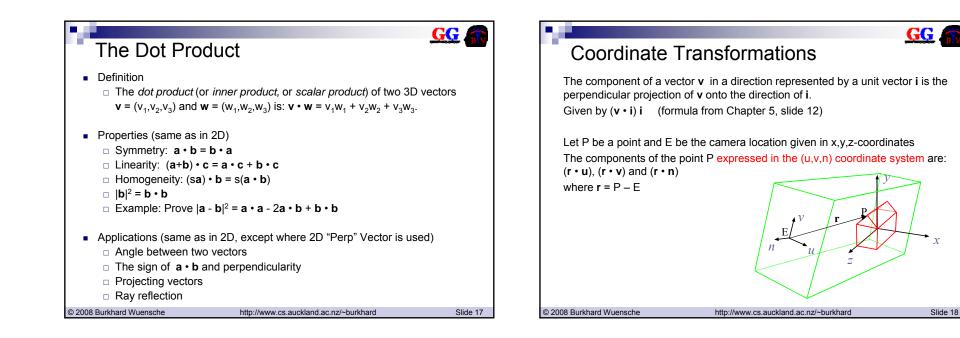
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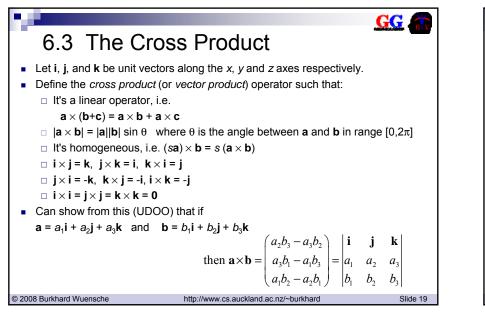


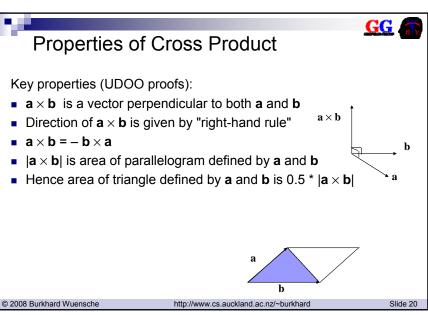


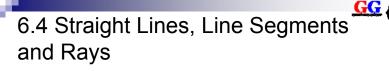












Use a *parametric* form for lines.
 Straight line through two points P₁ and P₂ is

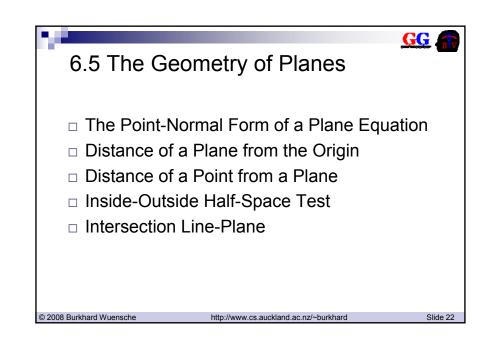
$$P(\alpha) = (1 - \alpha)P_1 + \alpha P_2$$
$$= P_1 + \alpha (P_2 - P_1)$$
$$= P_1 + \alpha \mathbf{v}$$

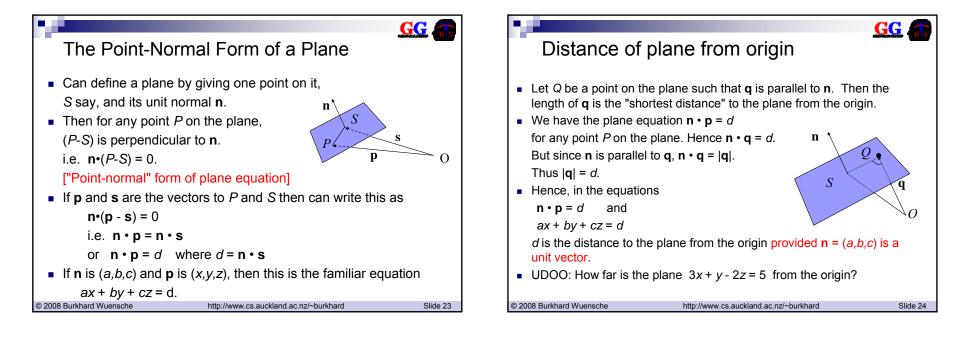
□ where **v** = P_2 - P_1 is the displacement vector from P_1 to P_2 .

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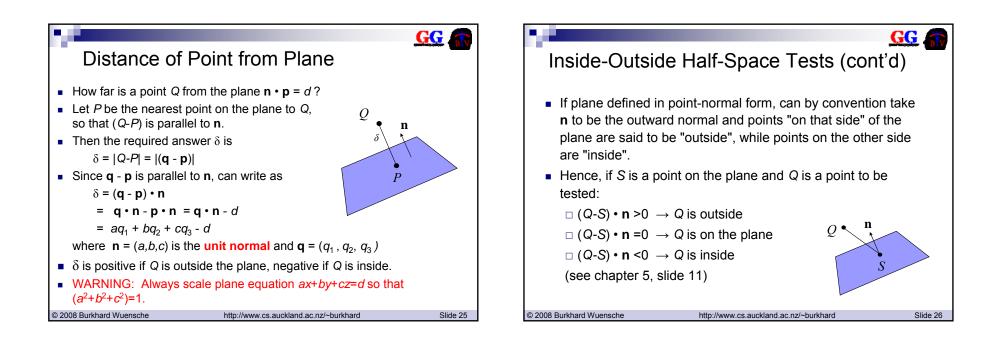
- If α constrained to the range [0,1] we have a *line segment* all points between P₁ and P₂.
- If α constrained to the range $[0,\infty]$ we have a *ray*.
- If α is any real number, we have a full line in *n*-space.

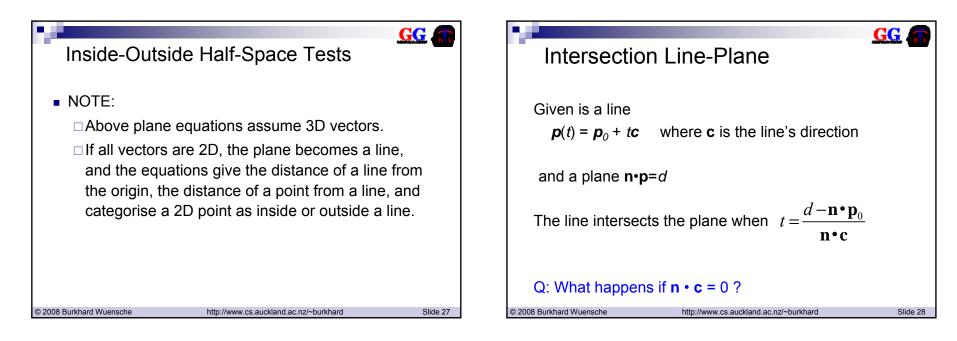
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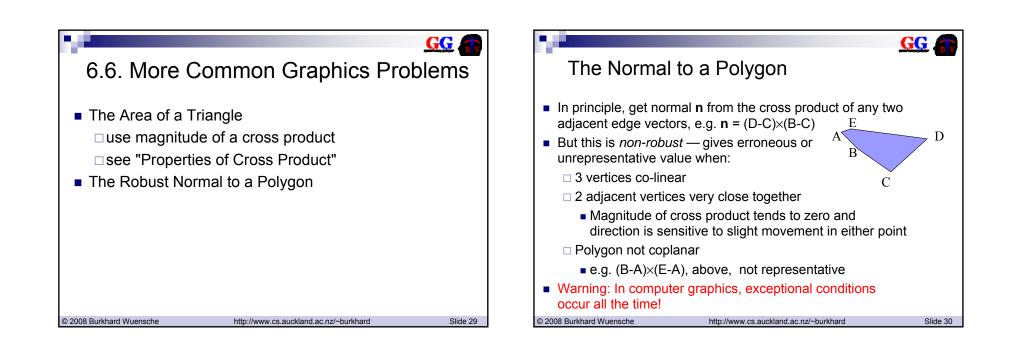


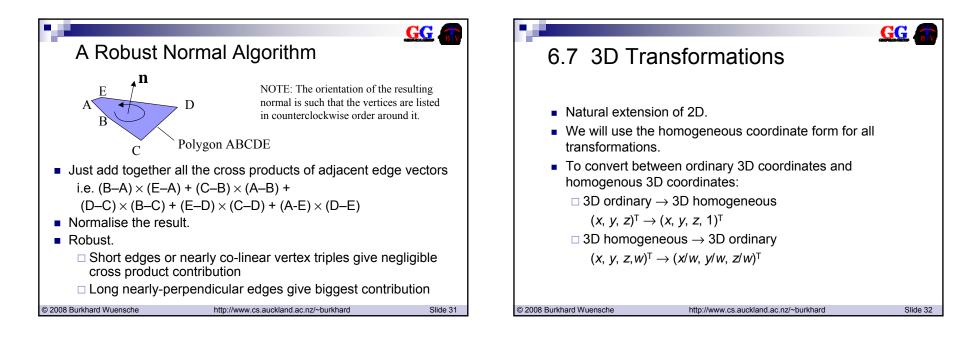


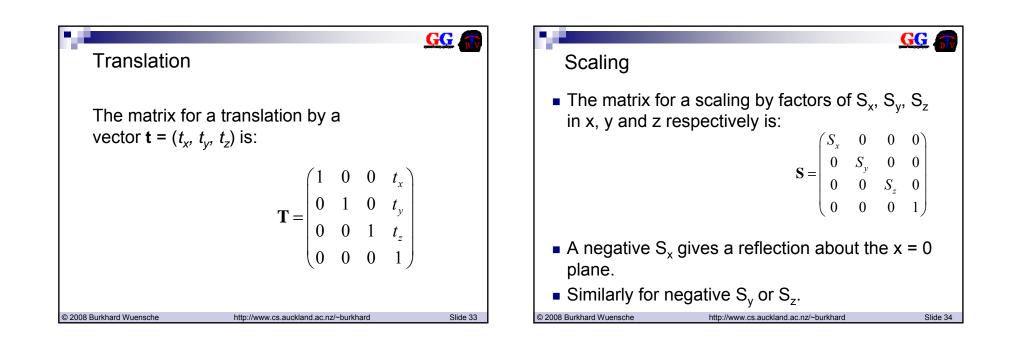
Slide 21

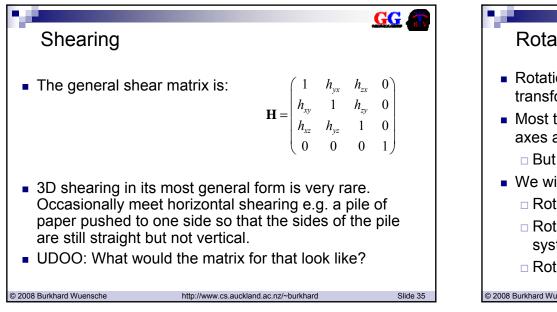




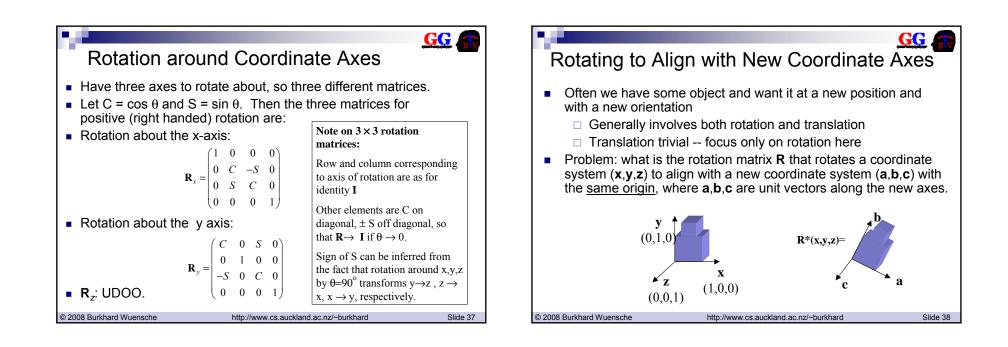






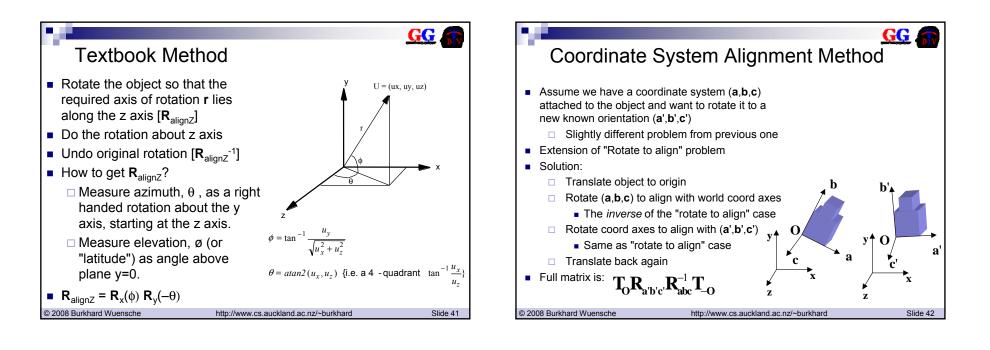


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Rotation		
 Rotations are b transformations 	by far the most confusing of the	
	er rotations around the three coor build all other rotations from thos	
But some ca	ses <i>very</i> difficult	
 We will conside 	er three different rotation situatior	IS:
Rotation area	und the three coordinate axes	
 Rotation to a system 	align an object with a new coordir	ate
Rotation area	und an arbitrary axis	
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Rotating to Aligr Axes (cont'd)	n with New Coordinate				
 To get R: we have R (1 0 0)^T = a R (0 1 0)^T = b R (0 0 1)^T = c 	$\mathbf{R} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} a_x & b_x & c_x \\ a_y & b_y & c_y \\ a_z & b_z & c_z \end{pmatrix}$				
 Above 3 eqns equivalent to: 					
$\therefore \mathbf{R} = \begin{pmatrix} a_x \\ a_y \\ a_z \end{pmatrix}$	$ \begin{array}{ccc} b_{x} & c_{x} \\ b_{y} & c_{y} \\ b_{z} & c_{z} \end{array} \right) \text{or} \ \mathbf{R}_{H.C.} = \begin{pmatrix} a_{x} & b_{x} & c_{x} & 0 \\ a_{y} & b_{y} & c_{y} & 0 \\ a_{z} & b_{z} & c_{z} & 0 \\ 0 & 0 & 0 & 1 \end{array} $				
 SO – IMPORTANT GENERAL RESULT: Columns of a 3 x 3 rotation matrix are unit vectors along the rotated coordinate axis directions UDOO – derive R_x, R_y, R_z from this rule. 					
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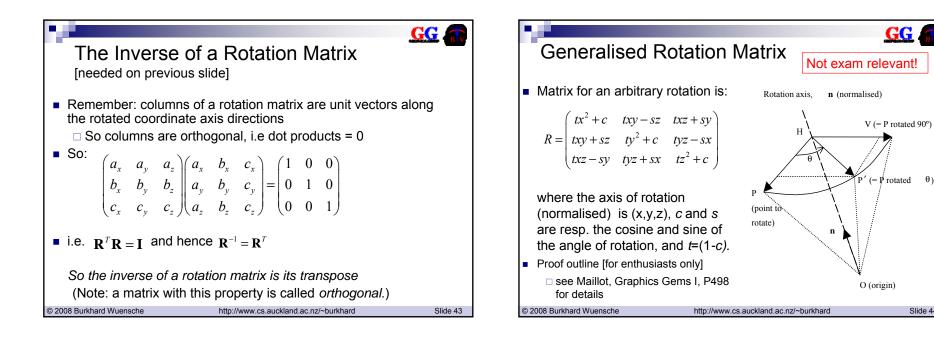
	Rotation about an arbitrary axis	
s a •	Often, when building a 3D scene or object, need to rotate a component aboresome arbitrary axis through a reference point on it. [e.g. forearm of robot rotaround an axis through the elbow]. Involves three steps: (1) Translate reference point to origin (2) Do the rotation (3) Translate reference point back again Three approaches for step (2) [next 3 slides]: Textbook method Decompose rotation into primitive rotations about x,y,z axes Nice exercise, but hard to get right in practice Coordinate system alignment method Generalised rotation matrix	
	An aside: Quaternions provide an elegant way of manipulating (axis, angle) rotations directly.	
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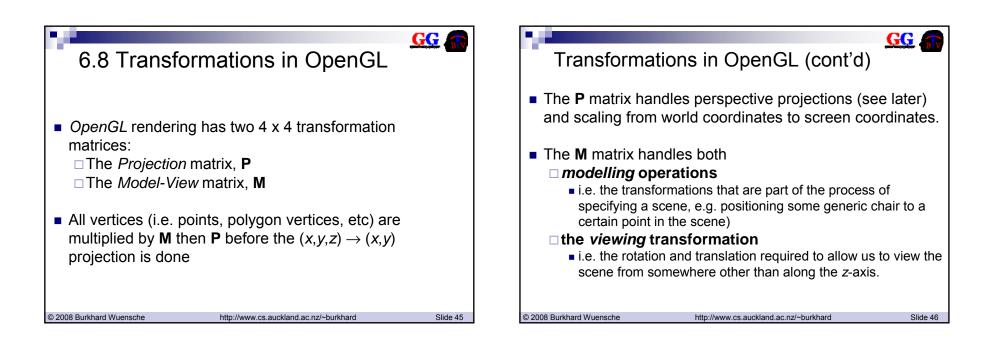


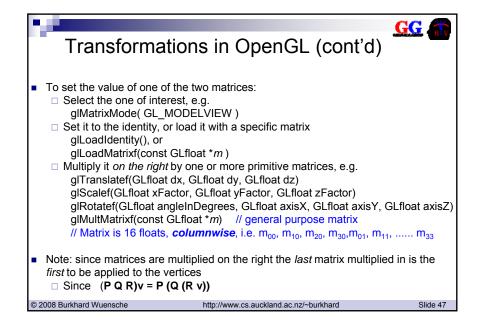
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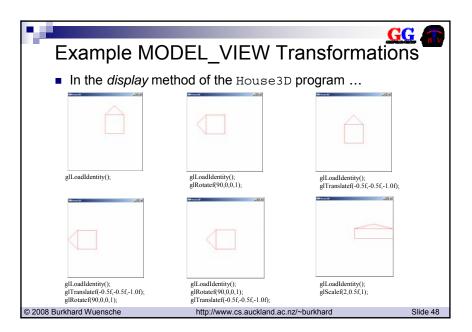
θ)

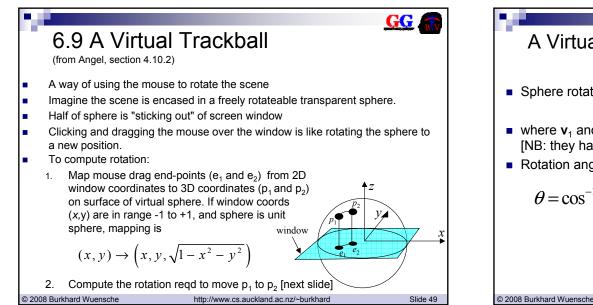
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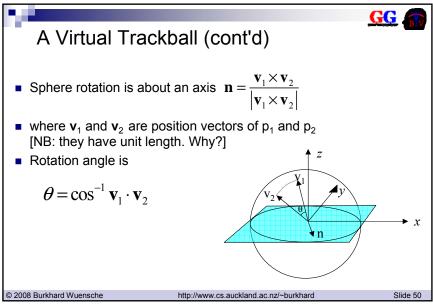




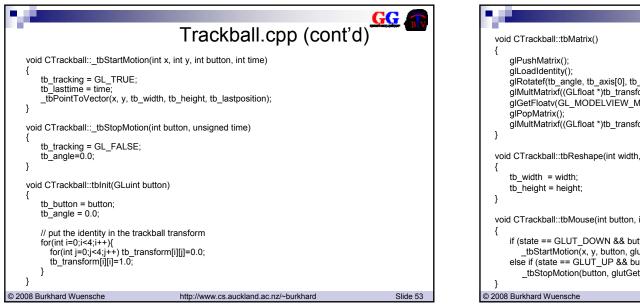


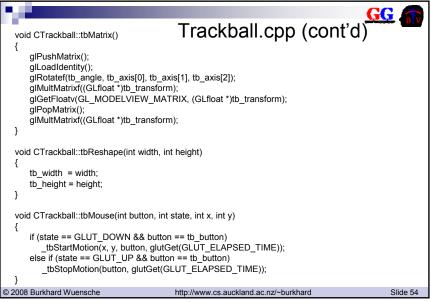






GLuint tb_width; GLuint tb_height; GLint tb_button; GLboolean tb_trackin	on[3]; // rotation axis and angle urrent rotation matrix for GL_MODEL_ // width and height of window g;		float d, a; // project x, y onto a hemi-sph v[0] = (float) ((2.0 * x - width) , v[1] = (float) ((height - 2.0 * y)	r(int x, int y, int width, int height, float v[3]){ ere centered within width, height. / width); / height);	<u>G</u>
	g; t height, float v[3]); ime);			/ height); 1] * v[1])); 5 / 2.0) * ((d < 1.0) ? d : 1.0)));	
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Trackball.cpp (cont'd)	void CTrackball::tbMotion(int x, int y){ GLfloat current_position[3], dx, dy, dz; if (tb_tracking == GL_FALSE) return;
<pre>void CTrackball::tbKeyboard(int key) { int i,j; for(i=0;i<4;i++) for(j=0;j<4;j++) tb_transform[i][j]=0.0; tb_transform[3][3]=1.0; switch (key) { case (int) 'z': tb_transform[0][0]=tb_transform[1][1]=tb_transform[2][2]=1.0; break; case (int) 'y': tb_transform[0][1]=tb_transform[1][2]=tb_transform[2][0]=1.0; break; case (int) 'x': tb_transform[0][2]=tb_transform[1][0]=tb_transform[2][1]=1.0; break; case (int) 'x': tb_transform[0][2]=tb_transform[1][0]=tb_transform[2][1]=1.0; break; default:; } // remember to draw new position glutPostRedisplay(); }</pre>	_tbPointToVector(x, y, tb_width, tb_height, current_position); // calculate the angle to rotate by (directly proportional to the // length of the mouse movement dx = current_position[0] - tb_lastposition[0]; dy = current_position[1] - tb_lastposition[2]; tb_angle = (float) (90.0 * sqrt(dx * dx + dy * dy + dz * dz)); // calculate the axis of rotation (cross product) tb_axis[0] = tb_lastposition[1] * current_position[2] - tb_lastposition[2] * current_position[1]; tb_axis[0] = tb_lastposition[2] * current_position[0] - tb_lastposition[0] * current_position[2]; tb_axis[2] = tb_lastposition[0] * current_position[1] - tb_lastposition[1] * current_position[0]; // reset for next time tb_lastformert time tb_lastposition[0] = current_position[0]; tb_lastposition[0] = current_position[1]; tb_lastposition[2] = current_position[2]; // remember to draw new position glutPostRedisplay(); }
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G	<u> 7</u>
#include <windows.h> House3DWithTrackball</windows.h>	
#include <gi gl.h=""></gi>	
#include <gl glu.h=""> #include <al glut.h=""></al></gl>	
#include <iostream></iostream>	
using namespace std; #include "Trackball.h"	
#Include Trackball.n	
const int windowWidth=400; const int windowHeight=400;	
// define vertices and edges of the house	
const int numVertices=10;	
const int numEdges=18;	
const float vertices[numVertices][3] = $\{\{0,0,0\},\{1,0,0\},\{0,1,0\},\{1,1,0\},\{0,0,2\},$	
{1,0,2},{0,1,2},{1,1,2},{0.5f,1.5f,0},{0.5f,1.5f,2}};	
const int edges[numEdges][2] = {{0,1},{1,3},{3,2},{2,0},{4,5},{5,7},{7,6},{6,4},{0,4},	
$\{1,5\},\{3,7\},\{2,6\},\{2,8\},\{8,3\},\{6,9\},\{9,7\},\{8,9\}\};$	
CTrackball trackball; // Add a trackball to our OpenGL program	
void handleMouseMotion(int x, int y){ trackball.tbMotion(x, y); }]
<pre>void handleMouseClick(int button, int state, int x, int y){ trackball.tbMouse(button, state, x, y);} void handleKeyboardEvent(unsigned char key, int x, int y){ trackball.tbKeyboard(key);}</pre>	
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