

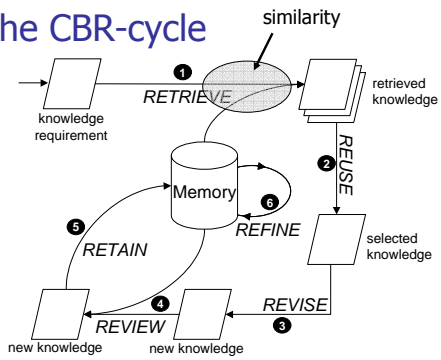


Case-Based Reasoning

Similarity / Diagnosis
Prof. Ian Watson



The CBR-cycle






Similarity ???

- Purpose of similarity, either:
 - Select cases that can be adapted easily to solve the current problem
 - Select cases that have (nearly) the same solution to the current problem
- Basic assumption:
 - similar problems have similar solutions

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Similarity ???

- Degree of similarity = utility or reusability of the solution
- Similarity is an *a priori* approximation of reusability
- Goal of similarity modelling:
 - provide a good approximation
 - close to real reusability
 - And easy to compute

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Similarity ???

- Assumptions
 - 2 similar problem descriptions have similar solution descriptions
 - It is easier to adapt the solution of a similar problem than the solution of a less similar problem

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Similarity ???

- Assumptions
 - 2 similar problem descriptions have similar solution descriptions
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Similarity ???

input problem description

Problem Space

Solution Space

- = description of new problem to solve
- = description of solved problems
- = stored solutions
- = new solution created by adaptation

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Modeling similarity

- Different approaches depending on case representation
- Similarity measures (metrics):
 - Functions to compare two cases:
 $sim(Case_1, Case_2) = [0..1]$
 - Local similarity measure: similarity on feature level
 - Global similarity measure: similarity on case or object level
 - combines local similarity measures
 - takes care of different importance of attributes (weights)

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Hamming distance

- A measure of the difference between two messages, each consisting of a finite string of characters, expressed by the number of characters that need to be changed to obtain one from the other.
- E.g., 0101 and 0110 has a Hamming distance of two

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Hamming distance

- In CBR each case feature in target case is compared to features of cases in entire case-base


Target case

Apples	Apples	Apples	case-base
Bread	Bread	Bread	
Eggs	Butter	Butter	
Beer	Beer	Wine	
Steak	Steak	Steak	

Hd $4/5 = 0.8$ $3/5 = 0.6$

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Hamming distance

- Problem - no attempt to indicate the importance or value of individual features


Target case

Apples	Apples	Apples	lager is a type of beer
Bread	Bread	Bread	
Eggs	Butter	Butter	
Beer	Beer	Lager	
Steak	Steak	Steak	

Hd $4/5 = 0.8$ $3/5 = 0.6$

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Similarity

- We therefore need more complex local similarity metrics
- $4 == 10?$ $\Delta = 6$
- $10 == 20?$ $\Delta = 10$
- $20 == 100?$ $\Delta = 80$
- Therefore the range is important & *outliers* are bad

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Similarity

- We therefore need more complex local similarity metrics
- $Sim = R - \Delta$
- $4 == 10?$ $\Delta = 100 - 6$ $Sim = 94\%$
- $10 == 20?$ $\Delta = 100 - 10$ $Sim = 90\%$
- $20 == 100?$ $\Delta = 100 - 80$ $Sim = 20\%$

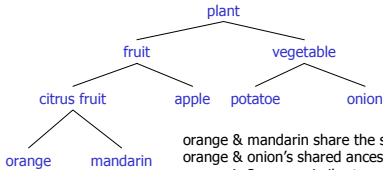
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Similarity

- Symbolic attributes are commonly modelled using symbol hierarchies



```


graph TD
    plant --> fruit
    plant --> vegetable
    fruit --> citrus_fruit[citrus fruit]
    fruit --> apple
    citrus_fruit --> orange
    citrus_fruit --> mandarin
    vegetable --> potatoe
    vegetable --> onion
  
```

orange & mandarin share the same parent (1 node higher)
 orange & onion's shared ancestor is 3 nodes higher
 orange is 3x more similar to mandarin than onion

orange == mandarin $Sim = 75\%$
 orange == onion $Sim = 25\%$

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Similarity Metrics

- We'll use CBR-Works as an exemplar
 - Symbols
 - Numbers
 - Intervals
 - Sets
 - Ordered sets
 - Strings
 - Taxonomy

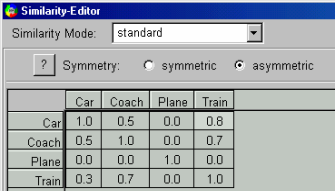
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Similarity


- Symbols (unordered)
 - Similarity defined by developer
 - Similarity values stored in a decision table



	Car	Coach	Plane	Train
Car	1.0	0.5	0.0	0.8
Coach	0.5	1.0	0.0	0.7
Plane	0.0	0.0	1.0	0.0
Train	0.3	0.7	0.0	1.0

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Similarity

- Symmetric vs asymmetric similarity
 - In symmetric similarity the result is independent of the role of the values being compared
 - $\text{Sim}(\text{Car}, \text{Train}) = 0.8$
 - $\text{Sim}(\text{Train}, \text{Car}) = 0.8$
 - In asymmetric similarity the role is important
 - $\text{Sim}(\text{Car}, \text{Train}) = 0.8$
 - $\text{Sim}(\text{Train}, \text{Car}) = 0.3$

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Similarity

- Numbers
 - Step function
 - Computes a *sim* of 1 if the difference is < step point otherwise a *sim* of 0
 - Polynomial function
 - Computes a *sim* between 0 & 1 using a polynomial curve (ie the closer to the query the greater the sim)
 - Function with a smooth step point
 - *sim* will be in (0.0; 1.0) in respect to the distance between query- and case-value.

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Similarity

- Perfect options
 - *Greater is perfect*
 - More horsepower
 - More days holiday
 - *Less is perfect*
 - Less money
 - Less time

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Similarity

- Intervals
 - if the intervals in query and case do not intersect the similarity is higher the closer the gap
 - if the intervals intersect the similarity is higher the closer the bounds
 - if the case completely covers the query the similarity is 1
 - if the query completely covers the case the similarity is higher the closer the bounds

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Similarity

- Sets – three similarity methods

Similarity	Description
intersection	The similarity computes to the proportion of the intersection of two SymbolSets to its union.
case-inclusion	The similarity equals to 1, if the case is included in the query. Entries included in case but not in query lower the similarity.
query-inclusion	The similarity equals to 1, if the query is included in the case. Entries included in query but not in case lower the similarity.

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Similarity

- Ordered Symbols
 - Similar to numbers
 - The symbols are mapped to a numeric range

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Similarity

- Strings
 - exact match - two strings are similar if they are spelled the same way
 - spelling check - compares the number of letters in two strings which are the same (Useful for strings consisting of one word only)
 - word-count - counts the number of matching words of two cases. (Useful for strings consisting of several words).

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Similarity


- Taxonomy
 - A classification hierarchy defines similarity for concepts
 - Inner nodes of the tree are assigned similarity values
 - Leaves under a node will share the nodes similarity

Taxonomy tree:

- [-] Arbitrary (0.3)
 - [-] City (0.5)
 - [-] Shopping
- [-] Education (0.5)
 - [-] Language
- [-] Recreation (0.6)
 - [-] Wandering
 - [-] Bathing
- [-] Active (0.5)
 - [-] Surfing
 - [-] Skiing
 - [-] Diving
 - [-] Adventure

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Retrieve, but efficiently ...

- Efficient case retrieval is essential for large case bases
- Different approaches depending on the:
 - case representation
 - size of the case base
- Organization of the case base:
 - Linear lists, only for small case bases
 - Index structures for large case bases
 - Kd-trees: index structure for large case bases (Wess)
 - Retrieval nets: index structure for textual (conversational) CBR (Lenz)

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Technical diagnosis

- Simple example: Car Faults
 - Symptoms are observed (e.g. engine doesn't start) and values are measured (e.g. battery voltage = 6.3V)
 - Goal: Find the cause for the failure (e.g. battery empty) and repair strategy (e.g. charge battery)
- Case-Based Diagnosis:
 - A case describes a diagnostic situation and contains:
 - description of the symptoms
 - description of the failure and the cause
 - description of a repair strategy

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Technical diagnosis

C A S E	Problem (Symptoms) <ul style="list-style-type: none"> • Problem: Front light doesn't work • Car: VW Golf II, 1.6 L • Year: 1993 • Battery voltage: 13.6 V • State of lights: OK • State of light switch: OK
	Solution <ul style="list-style-type: none"> • Diagnosis: Front light fuse defect • Repair: Replace front light fuse

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Each case describes one situation

Cases are independent of each other


Cases are not rules

CASE	Problem (Symptoms)	<ul style="list-style-type: none">Problem: Front light doesn't workCar: VW Golf II, 1.6 LYear: 1993Battery voltage: 13,6 VState of lights: OKState of light switch: OK
	1 Solution	<ul style="list-style-type: none">Diagnosis: Front light fuse defectRepair: Replace front light fuse

CASE	Problem (Symptoms)	<ul style="list-style-type: none">Problem: Front light doesn't workCar: Audi A6Year: 1995Battery voltage: 12,9 VState of lights: surface damagedState of light switch: OK
	2 Solution	<ul style="list-style-type: none">Diagnosis: Bulb defectRepair: Replace front light

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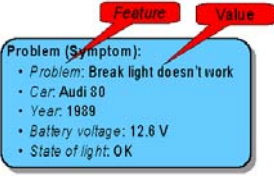
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Solving a diagnostic problem

- Make several observations about new problem
- Not all features must be known
- The new problem is a case without the solution part




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Solving a diagnostic problem



- Compare the new problem with each case & select most similar case
- Similarity* is the most important concept in CBR

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Similarity

- Similarity is assessed for each feature
- Depends on the feature value
- Features can have different weights (importance)

- Feature: *Problem*

Front light doesn't work $\xleftarrow{0.8}$ Break light doesn't work
 Front light doesn't work $\xleftarrow{0.4}$ Engine doesn't start

- Feature: *Battery voltage* (similarity depends on the difference)

12.6 V $\xleftarrow{0.9}$ 13.6 V
 12.6 V $\xleftarrow{0.1}$ 6.7 V

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Similarity

- Different features have different importance
- High importance:
Problem: Battery_voltage: State_of_light:
- Low importance:
Make: Model: Year: Colour:

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Compare new problem with case 1

Problem (Symptom)

- Prob.: Break light doesn't work
- Car: Audi 80
- Year: 1989
- Battery voltage: 12.6 V
- State of lights: OK

Problem (Symptoms)

- Problem: Front light doesn't work
- Car: VW Golf II, 1.6 L
- Year: 1993
- Battery voltage: 13.6 V
- State of lights: OK
- State of light switch: OK

Solution

- Diagnosis: Front light fuse defect
- Repair: Replace front light fuse

Very important feature: weight = 6 \leftrightarrow
 Less important feature: weight = 1 \leftrightarrow

Similarity Computation by Weighted Average

$similarity(new_case\ 1) = 1/20 * [6*0.8 + 1*0.4 + 1*0.6 + 6*0.9 + 6*1.0] = 0.86$

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Compare new problem with case 2

Problem (Symptom)

- Prob.: Break light doesn't work
- Car: Audi 80
- Year: 1989
- Battery voltage: 12.6 V
- State of lights: OK

Problem (Symptoms)

- Problem: Front light doesn't work
- Car: Audi A6
- Year: 1995
- Battery voltage : 12.9 V
- State of lights: surface damaged
- State of light switch: OK

Solution

- Diagnosis: Bulb defect
- Repair: Replace front light

Very important feature: weight = 6 ↔
 Less important feature: weight = 1 ↔

Similarity Computation by Weighted Average

$$\text{similarity}(\text{new}, \text{case 2}) = 1/20 * [6*0.8 + 1*0.8 + 1*0.4 + 6*0.95 + 6*0] = 0.585$$

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Reuse the Solution of Case 1

CASE 1

Problem (Symptoms):

- Front light doesn't work
- ...

Solution:

- Diagnosis: Front light fuse defect
- Repair: Replace front light fuse

Problem (Symptom):

- Prob.: Break light doesn't work
- Car: Audi 80
- Year: 1989
- Battery voltage: 12,6 V
- state of break light: OK

Adapt Solution:
How do differences in the problem affect the solution?

New Solution:

- Diagnosis: Break light fuse defect
- Repair: Replace break light fuse

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Store the New Experience

If diagnosis is correct:
store new case in the memory.
(retain)

CASE 3

Problem (Symptoms):

- Problem: Break light doesn't work
- Car: Audi 80
- Year: 1989
- Battery voltage: 12.6 V
- State of break lights: OK
- light switch clicking: OK

Solution:

- Diagnosis: break light fuse defect
- Repair: replace break light fuse

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